Gravimetric Methods

Chapter Overview

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Gravimetry includes all analytical methods in which the analytical signal is a measurement of mass or a change in mass. When you step on a scale after exercising you are making, in a sense, a gravimetric determination of your mass. Mass is the most fundamental of all analytical measurements, and gravimetry is unquestionably our oldest quantitative analytical technique. The publication in 1540 of Vannoccio Biringuccio’s *Pirotechnia* is an early example of applying gravimetry—although not yet known by this name—to the analysis of metals and ores.\(^1\) Although gravimetry no longer is the most important analytical method, it continues to find use in specialized applications.

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8A Overview of Gravimetric Methods

Before we consider specific gravimetric methods, let’s take a moment to develop a broad survey of gravimetry. Later, as you read through the descriptions of specific gravimetric methods, this survey will help you focus on their similarities instead of their differences. You will find that it is easier to understand a new analytical method when you can see its relationship to other similar methods.

8A.1 Using Mass as an Analytical Signal

Suppose you are to determine the total suspended solids in the water released by a sewage-treatment facility. Suspended solids are just that—solid matter that has yet to settle out of its solution matrix. The analysis is easy. After collecting a sample, you pass it through a preweighed filter that retains the suspended solids, and dry the filter and solids to remove any residual moisture. The mass of suspended solids is the difference between the filter’s final mass and its original mass. We call this a direct analysis because the analyte—the suspended solids in this example—is the species that is weighed.

What if our analyte is an aqueous ion, such as Pb$^{2+}$? Because the analyte is not a solid, we cannot isolate it by filtration. We can still measure the analyte’s mass directly if we first convert it into a solid form. If we suspend a pair of Pt electrodes in the sample and apply a sufficiently positive potential between them for a long enough time, we can force the following reaction to completion.

\[
Pb^{2+}(aq) + 4H_2O(l) \rightleftharpoons PbO_2(s) + H_2(g) + 2H_3O^+(aq)
\]

Oxidizing Pb$^{2+}$ deposits PbO$_2$ on the Pt anode. If we weigh the anode before and after applying the potential, the change in its mass gives the mass of PbO$_2$ and, from the reaction’s stoichiometry, the amount of Pb$^{2+}$ in the sample. This is a direct analysis because PbO$_2$ contains the analyte.

Sometimes it is easier to remove the analyte and let a change in mass serve as the analytical signal. Suppose you need to determine a food’s moisture content. One approach is to heat a sample of the food to a temperature that vaporizes the water, capturing it in a preweighed absorbent trap. The change in the absorbent’s mass provides a direct determination of the amount of water in the sample. An easier approach is to weigh the sample of food before and after heating, using the change in its mass as an indication of the amount of water originally present. We call this an indirect analysis because we determine the analyte using a signal that is proportional to its disappearance.

The indirect determination of a sample’s moisture content is done by difference. The sample’s initial mass includes the water, but its final mass does not. We can also determine an analyte indirectly without its ever being...
weighed. For example, phosphite, $PO_3^{3-}$, reduces $Hg^{2+}$ to $Hg_2^{2+}$, which in the presence of $Cl^-$ precipitates as $Hg_2Cl_2$.

$$2HgCl_2(aq) + PO_3^{3-}(aq) + 3H_2O(l) \rightleftharpoons Hg_2Cl_2(s) + 2H_3O^+(aq) + 2Cl^-(aq) + 2PO_4^{3-}(aq)$$

If we add $HgCl_2$ in excess, each mole of $PO_3^{3-}$ produces one mole of $Hg_2Cl_2$. The precipitate's mass, therefore, provides an indirect measurement of the amount of $PO_3^{3-}$ in the original sample.

### 8A.2 Types of Gravimetric Methods

The four examples in the previous section illustrate different ways in which the measurement of mass may serve as an analytical signal. When the signal is the mass of a precipitate, we call the method **precipitation gravimetry**. The indirect determination of $PO_3^{3-}$ by precipitating $Hg_2Cl_2$ is an example, as is the direct determination of $Cl^-$ by precipitating $AgCl$.

In **electrogravimetry**, we deposit the analyte as a solid film on an electrode in an electrochemical cell. The deposition as $PbO_2$ at a Pt anode is one example of electrogravimetry. The reduction of $Cu^{2+}$ to $Cu$ at a Pt cathode is another example of electrogravimetry.

When we use thermal or chemical energy to remove a volatile species, we call the method **volatilization gravimetry**. In determining the moisture content of bread, for example, we use thermal energy to vaporize the water in the sample. To determine the amount of carbon in an organic compound, we use the chemical energy of combustion to convert it to $CO_2$.

Finally, in **particulate gravimetry** we determine the analyte by separating it from the sample’s matrix using a filtration or an extraction. The determination of total suspended solids is one example of particulate gravimetry.

### 8A.3 Conservation of Mass

An accurate gravimetric analysis requires that the analytical signal—whether it is a mass or a change in mass—be proportional to the amount of analyte in our sample. For all gravimetric methods this proportionality involves a **conservation of mass**. If the method relies on one or more chemical reactions, then the stoichiometry of the reactions must be known. Thus, for the analysis of $PO_3^{3-}$ described earlier, we know that each mole of $Hg_2Cl_2$ corresponds to a mole of $PO_3^{3-}$ in our sample. If we remove the analyte from its matrix, then the separation must be selective for the analyte. When determining the moisture content in bread, for example, we know that the mass of $H_2O$ in the bread is the difference between the sample's final mass and its initial mass.

We will not consider electrogravimetry in this chapter. See Chapter 11 on electrochemical methods of analysis for a further discussion of electrogravimetry.

We will return to this concept of applying a conservation of mass later in the chapter when we consider specific examples of gravimetric methods.
8A.4 Why Gravimetry is Important

Except for particulate gravimetry, which is the most trivial form of gravimetry, you probably will not use gravimetry after you complete this course. Why, then, is familiarity with gravimetry still important? The answer is that gravimetry is one of only a small number of DEFINITIVE TECHNIQUES whose measurements require only base SI units, such as mass or the mole, and defined constants, such as Avogadro’s number and the mass of $^{12}\text{C}$. Ultimately, we must be able to trace the result of an analysis to a definitive technique, such as gravimetry, that we can relate to fundamental physical properties. Although most analysts never use gravimetry to validate their results, they often verifying an analytical method by analyzing a standard reference material whose composition is traceable to a definitive technique.

8B Precipitation Gravimetry

In precipitation gravimetry an insoluble compound forms when we add a precipitating reagent, or PRECIPITANT, to a solution containing our analyte. In most methods the precipitate is the product of a simple metathesis reaction between the analyte and the precipitant; however, any reaction generating a precipitate can potentially serve as a gravimetric method.

8B.1 Theory and Practice

All precipitation gravimetric analysis share two important attributes. First, the precipitate must be of low solubility, of high purity, and of known composition if its mass is to accurately reflect the analyte’s mass. Second, the precipitate must be easy to separate from the reaction mixture.

Solubility Considerations

To provide accurate results, a precipitate’s solubility must be minimal. The accuracy of a total analysis technique typically is better than ±0.1%, which means that the precipitate must account for at least 99.9% of the analyte. Extending this requirement to 99.99% ensures that the precipitate’s solubility does not limit the accuracy of a gravimetric analysis.

We can minimize solubility losses by carefully controlling the conditions under which the precipitate forms. This, in turn, requires that we account for every equilibrium reaction affecting the precipitate’s solubility. For example, we can determine Ag⁺ gravimetrically by adding NaCl as a precipitant, forming a precipitate of AgCl.

$$\text{Ag}^+(aq) + \text{Cl}^-(aq) \rightleftharpoons \text{AgCl(s)}$$ \hspace{1cm} 8.1

If this is the only reaction we consider, then we predict that the precipitate’s solubility, $S_{\text{AgCl}}$, is given by the following equation.


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Equation 8.2 suggests that we can minimize solubility losses by adding a large excess of Cl\(^-\). In fact, as shown in Figure 8.1, adding a large excess of Cl\(^-\) increases the precipitate's solubility.

To understand why the solubility of AgCl is more complicated than the relationship suggested by equation 8.2, we must recognize that Ag\(^+\) also forms a series of soluble silver-chloro metal–ligand complexes.

\[
\text{Ag}^+ (aq) + \text{Cl}^- (aq) \rightleftharpoons \text{AgCl}(aq) \quad \log K_1 = 3.70 \quad 8.3
\]

\[
\text{AgCl}(aq) + \text{Cl}^- (aq) \rightleftharpoons \text{AgCl}_2 (aq) \quad \log K_2 = 1.92 \quad 8.4
\]

\[
\text{AgCl}_2 (aq) + \text{Cl}^- (aq) \rightleftharpoons \text{AgCl}_3^- (aq) \quad \log K_3 = 0.78 \quad 8.5
\]

The actual solubility of AgCl is the sum of the equilibrium concentrations for all soluble forms of Ag\(^+\), as shown by the following equation.

\[
S_{\text{AgCl}} = [\text{Ag}^+] + [\text{AgCl}(aq)] + [\text{AgCl}_2] + [\text{AgCl}_3^-] \quad 8.6
\]

By substituting into equation 8.6 the equilibrium constant expressions for reaction 8.1 and reactions 8.3–8.5, we can define the solubility of AgCl as

\[
S_{\text{AgCl}} = \frac{K_p}{[\text{Cl}^-]} + K_1 [\text{Cl}^-] + K_1 K_2 [\text{Cl}^-]^2 + K_1 K_2 K_3 [\text{Cl}^-]^3 \quad 8.7
\]

Equation 8.7 explains the solubility curve for AgCl shown in Figure 8.1. As we add NaCl to a solution of Ag\(^+\), the solubility of AgCl initially decreas-

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**Figure 8.1** Solubility of AgCl as a function of pCl. The dashed red line shows our prediction for \(S_{\text{AgCl}}\) if we incorrectly assume that only reaction 8.1 and equation 8.2 affect silver chloride’s solubility. The solid blue curve is calculated using equation 8.7, which accounts for reaction 8.1 and reactions 8.3–8.5. Because the solubility of AgCl spans several orders of magnitude, \(S_{\text{AgCl}}\) is displayed on the y-axis in logarithmic form.

**Problem 1** in the end-of-chapter problems asks you to show that equation 8.7 is correct by completing the derivation.
The predominate silver-chloro complexes for different values of pCl are shown by the ladder diagram along the x-axis in Figure 8.1. Note that the increase in solubility begins when the higher-order soluble complexes, AgCl$_2^-$ and AgCl$_3^{2-}$, become the predominate species.

Be sure that equation 8.10 makes sense to you. Reaction 8.8 tells us that the dissolution of CaF$_2$ produces one mole of Ca$^{2+}$ for every two moles of F$^-$, which explains the term of 1/2 in equation 8.10. Because F$^-$ is a weak base, we need to account for both of its chemical forms in solution, which explains why we include HF.

Problem 4 in the end-of-chapter problems asks you to show that equation 8.11 is correct by completing the derivation.

Figure 8.2 shows how pH affects the solubility of CaF$_2$. Depending on the solution’s pH, the predominate form of fluoride is either HF or F$^-$. When the pH is greater than 4.17, the predominate species is F$^-$ and the solubility of CaF$_2$ is independent of pH because only reaction 8.8 occurs to an ap-

es because of reaction 8.1. Under these conditions, the final three terms in equation 8.7 are small and equation 8.1 is sufficient to describe AgCl’s solubility. At higher concentrations of Cl$^-$, reaction 8.4 and reaction 8.5 increase the solubility of AgCl. Clearly the equilibrium concentration of chloride is important if we want to determine the concentration of silver by precipitating AgCl. In particular, we must avoid a large excess of chloride.

Another important parameter that may affect a precipitate’s solubility is pH. For example, a hydroxide precipitates such as Fe(OH)$_3$ is more soluble at lower pH levels where the concentration of OH$^-$ is small. Because fluoride is a weak base, the solubility of calcium fluoride, $S_{CaF_2}$, also is pH-dependent. We can derive an equation for $S_{CaF_2}$ by considering the following equilibrium reactions

$$CaF_2(s) \rightleftharpoons Ca^{2+}(aq) + 2F^-(aq) \quad K_w = 3.9 \times 10^{-11} \quad 8.8$$

$$HF(aq) + H_2O(l) \rightleftharpoons H_3O^+(aq) + F^-(aq) \quad K_a = 6.8 \times 10^{-4} \quad 8.9$$

and the following equation for the solubility of CaF$_2$.

$$S_{CaF_2} = [Ca^{2+}] = \frac{1}{2} \left\{ [F^-] + [HF] \right\} \quad 8.10$$

Substituting the equilibrium constant expressions for reaction 8.8 and reaction 8.9 into equation 8.10 defines the solubility of CaF$_2$ in terms of the equilibrium concentration of H$_3$O$^+$.

$$S_{CaF_2} = [Ca^{2+}] = \left\{ \frac{K_w}{4} \left( 1 + \frac{[H_3O^+]}{K_a} \right) \right\}^{1/3} \quad 8.11$$

Figure 8.2 shows how pH affects the solubility of CaF$_2$. Depending on the solution’s pH, the predominate form of fluoride is either HF or F$^-$. When the pH is greater than 4.17, the predominate species is F$^-$ and the solubility of CaF$_2$ is independent of pH because only reaction 8.8 occurs to an ap-
preciable extent. At more acidic pH levels, the solubility of CaF$_2$ increases because of the contribution of reaction 8.9.

When solubility is a concern, it may be possible to decrease solubility by using a non-aqueous solvent. A precipitate’s solubility is generally greater in an aqueous solution because of water’s ability to stabilize ions through solvation. The poorer solvating ability of non-aqueous solvents, even those which are polar, leads to a smaller solubility product. For example, the $K_{sp}$ of PbSO$_4$ is $2 \times 10^{-8}$ in H$_2$O and $2.6 \times 10^{-12}$ in a 50:50 mixture of H$_2$O and ethanol.

**AVOIDING IMPURITIES**

In addition to having a low solubility, the precipitate must be free from impurities. Because precipitation usually occurs in a solution that is rich in dissolved solids, the initial precipitate is often impure. We must remove these impurities before determining the precipitate’s mass.

The greatest source of impurities is the result of chemical and physical interactions occurring at the precipitate’s surface. A precipitate is generally crystalline—even if only on a microscopic scale—with a well-defined lattice of cations and anions. Those cations and anions at the precipitate’s surface carry, respectively, a positive or a negative charge because they have incomplete coordination spheres. In a precipitate of AgCl, for example, each silver ion in the precipitate’s interior is bound to six chloride ions. A silver ion at the surface, however, is bound to no more than five chloride ions and carries a partial positive charge (Figure 8.3). The presence of these partial charges makes the precipitate’s surface an active site for the chemical and physical interactions that produce impurities.

One common impurity is an **INCLUSION**. A potential interfering ion whose size and charge is similar to a lattice ion, may substitute into the

**Practice Exercise 8.1**

You can use a ladder diagram to predict the conditions for minimizing a precipitate’s solubility. Draw a ladder diagram for oxalic acid, H$_2$C$_2$O$_4$, and use it to establish a suitable range of pH values for minimizing the solubility of CaC$_2$O$_4$. Relevant equilibrium constants may be found in the appendices.

Click [here](#) to review your answer to this exercise.

![Ball-and-stick diagram showing the lattice structure of AgCl](image)

Figure 8.3 Ball-and-stick diagram showing the lattice structure of AgCl. Each silver ion in the lattice’s interior binds with six chloride ions, and each chloride ion in the interior binds with six silver ions. Those ions on the lattice’s surface or edges bind to fewer than six ions and carry a partial charge. A silver ion on the surface, for example, carries a partial positive charge. These charges make the surface of a precipitate an active site for chemical and physical interactions.
An inclusion is difficult to remove since it is chemically part of the precipitate’s lattice. The only way to remove an inclusion is through reprecipitation. After isolating the precipitate from its supernatant solution, we dissolve it by heating in a small portion of a suitable solvent. We then allow the solution to cool, reforming the precipitate. Because the interferent’s concentration is less than that in the original solution, the amount of included material is smaller. We can repeat the process of reprecipitation until the inclusion’s mass is insignificant. The loss of analyte during reprecipitation, however, can be a significant source of error.

Oclusions form when interfering ions become trapped within the growing precipitate. Unlike inclusions, which are randomly dispersed within the precipitate, an occlusion is localized, either along flaws within the precipitate’s lattice structure or within aggregates of individual precipitate particles (Figure 8.4b). An occlusion usually increases a precipitate’s mass; however, the mass is smaller if the occlusion includes the analyte in a lower molecular weight form than that of the precipitate.

We can minimize occlusions by maintaining the precipitate in equilibrium with its supernatant solution for an extended time. This process is called a digestion. During digestion, the dynamic nature of the solubility–precipitation equilibrium, in which the precipitate dissolves and reforms, ensures that the occlusion is reexposed to the supernatant solution. Because
the rates of dissolution and reprecipitation are slow, there is less opportunity for forming new occlusions.

After precipitation is complete the surface continues to attract ions from solution (Figure 8.4c). These **surface adsorbates** comprise a third type of impurity. We can minimize surface adsorption by decreasing the precipitate’s available surface area. One benefit of digesting a precipitate is that it increases the average particle size. Because the probability of a particle completely dissolving is inversely proportional to its size, during digestion larger particles increase in size at the expense of smaller particles. One consequence of forming a smaller number of larger particles is an overall decrease in the precipitate’s surface area. We also can remove surface adsorbates by washing the precipitate, although the potential loss of analyte cannot be ignored.

Inclusions, occlusions, and surface adsorbates are examples of **coprecipitates**—otherwise soluble species that form within the precipitate containing the analyte. Another type of impurity is an interferent that forms an independent precipitate under the conditions of the analysis. For example, the precipitation of nickel dimethylglyoxime requires a slightly basic pH. Under these conditions, any Fe$^{3+}$ in the sample precipitates as Fe(OH)$_3$. In addition, because most precipitants are rarely selective toward a single analyte, there is always a risk that the precipitant will react with both the analyte and an interferent.

We can minimize the formation of additional precipitates by carefully controlling solution conditions. If an interferent forms a precipitate that is less soluble than the analyte’s precipitate, we can precipitate the interferent and remove it by filtration, leaving the analyte behind in solution. Alternatively, we can mask the analyte or the interferent to prevent its precipitation.

Both of the above-mentioned approaches are illustrated in Fresenius’ analytical method for determining Ni in ores containing Pb$^{2+}$, Cu$^{2+}$, and Fe$^{3+}$ (see Figure 1.1 in Chapter 1). Dissolving the ore in the presence of H$_2$SO$_4$ selectively precipitates Pb$^{2+}$ as PbSO$_4$. Treating the supernatant with H$_2$S precipitates the Cu$^{2+}$ as CuS. After removing the CuS by filtration, adding ammonia precipitates Fe$^{3+}$ as Fe(OH)$_3$. Nickel, which forms a soluble amine complex, remains in solution.

**CONTROLLING PARTICLE SIZE**

Size matters when it comes to forming a precipitate. Larger particles are easier to filter, and, as noted earlier, a smaller surface area means there is less opportunity for surface adsorbates to form. By carefully controlling the reaction conditions we can significantly increase a precipitate’s average particle size.

Precipitation consists of two distinct events: nucleation, the initial formation of smaller stable particles of precipitate, and particle growth. Larger particles form when the rate of particle growth exceeds the rate of nucleation.
A supersaturated solution is one that contains more dissolved solute than that predicted by equilibrium chemistry. The solution is inherently unstable and precipitates solute to reach its equilibrium position. How quickly this process occurs depends, in part, on the value of $RSS$.

Understanding the conditions favoring particle growth is important when designing a gravimetric method of analysis.

We define a solute’s RELATIVE SUPERSATURATION, $RSS$, as

$$RSS = \frac{Q-S}{S}$$  \hspace{1cm} 8.12

where $Q$ is the solute’s actual concentration and $S$ is the solute’s concentration at equilibrium. The numerator of equation 8.12, $Q-S$, is a measure of the solute’s supersaturation. A solution with a large, positive value of $RSS$ has a high rate of nucleation, producing a precipitate with many small particles. When the $RSS$ is small, precipitation is more likely to occur by particle growth than by nucleation.

Examining equation 8.12 shows that we can minimize $RSS$ by decreasing the solute’s concentration, $Q$, or by increasing the precipitate’s solubility, $S$. A precipitate’s solubility usually increases at higher temperatures, and adjusting pH may affect a precipitate’s solubility if it contains an acidic or a basic ion. Temperature and pH, therefore, are useful ways to increase the value of $S$. Conducting the precipitation in a dilute solution of analyte, or adding the precipitant slowly and with vigorous stirring are ways to decrease the value of $Q$.

There are practical limitations to minimizing $RSS$. Some precipitates, such as Fe(OH)$_3$ and PbS, are so insoluble that $S$ is very small and a large $RSS$ is unavoidable. Such solutes inevitably form small particles. In addition, conditions favoring a small $RSS$ may lead to a relatively stable supersaturated solution that requires a long time to fully precipitate. For example, almost a month is required to form a visible precipitate of BaSO$_4$ under conditions in which the initial $RSS$ is 5.

A visible precipitate takes longer to form when $RSS$ is small both because there is a slow rate of nucleation and because there is a steady decrease in $RSS$ as the precipitate forms. One solution to the latter problem is to generate the precipitant in situ as the product of a slow chemical reaction. This maintains the $RSS$ at an effectively constant level. Because the precipitate forms under conditions of low $RSS$, initial nucleation produces a small number of particles. As additional precipitant forms, particle growth supersedes nucleation, resulting in larger precipitate particles. This process is called HOMOGENEOUS PRECIPITATION.

Two general methods are used for homogeneous precipitation. If the precipitate’s solubility is pH-dependent, then we can mix the analyte and the precipitant under conditions where precipitation does not occur, and then increase or decrease the pH by chemically generating OH$^-$ or H$_3$O$^+$. For example, the hydrolysis of urea is a source of OH$^-$.  

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\[
\text{CO(NH}_2\text{)}_2(aq) + \text{H}_2\text{O}(l) \rightleftharpoons 2\text{NH}_3(aq) + \text{CO}_2(g)
\]

\[
\text{NH}_3(aq) + \text{H}_2\text{O}(l) \rightleftharpoons \text{OH}^-(aq) + \text{NH}_4^+(aq)
\]

Because the hydrolysis of urea is temperature-dependent—it is negligible at room temperature—we can use temperature to control the rate of hydrolysis and the rate of precipitate formation. Precipitates of \(\text{CaC}_2\text{O}_4\), for example, have been produced by this method. After dissolving the sample containing \(\text{Ca}^{2+}\), the solution is made acidic with \(\text{HCl}\) before adding a solution of 5% \(\text{w/v } (\text{NH}_4\text{)}_2\text{C}_2\text{O}_4\). Because the solution is acidic, a precipitate of \(\text{CaC}_2\text{O}_4\) does not form. The solution is heated to approximately 50°C and urea is added. After several minutes, a precipitate of \(\text{CaC}_2\text{O}_4\) begins to form, with precipitation reaching completion in about 30 min.

In the second method of homogeneous precipitation, the precipitant is generated by a chemical reaction. For example, \(\text{Pb}^{2+}\) is precipitated homogeneously as \(\text{PbCrO}_4\) by using bromate, \(\text{BrO}_3^-\), to oxidize \(\text{Cr}^{3+}\) to \(\text{CrO}_4^{2-}\).

\[
6\text{BrO}_3^-(aq) + 10\text{Cr}^{3+}(aq) + 22\text{H}_2\text{O}(l) \rightleftharpoons 3\text{Br}_2(aq) + 10\text{CrO}_4^{2-}(aq) + 44\text{H}^+(aq)
\]

Figure 8.5 shows the result of preparing \(\text{PbCrO}_4\) by the direct addition of \(\text{KCrO}_4\) (Beaker A) and by homogenous precipitation (Beaker B). Both beakers contain the same amount of \(\text{PbCrO}_4\). Because the direct addition of \(\text{KCrO}_4\) leads to rapid precipitation and the formation of smaller particles, the precipitate remains less settled than the precipitate prepared homogeneously. Note, as well, the difference in the color of the two precipitates.

A homogeneous precipitation produces large particles of precipitate that are relatively free from impurities. These advantages, however, are offset by requiring more time to produce the precipitate and a tendency for the precipitate to deposit as a thin film on the container’s walls. The latter problem is particularly severe for hydroxide precipitates generated using urea.

An additional method for increasing particle size deserves mention. When a precipitate’s particles are electrically neutral they tend to coagulate

Figure 8.5 Two precipitates of \(\text{PbCrO}_4\). In Beaker A, combining 0.1 M \(\text{Pb(NO}_3\text{)}_2\) and 0.1 M \(\text{K}_2\text{CrO}_4\) forms the precipitate under conditions of high \(\text{RSS}\). The precipitate forms rapidly and consists of very small particles. In Beaker B, heating a solution of 0.1 M \(\text{Pb(NO}_3\text{)}_2\), 0.1 M \(\text{Cr(NO}_3\text{)}_3\), and 0.1 M \(\text{KBrO}_3\) slowly oxidizes \(\text{Cr}^{3+}\) to \(\text{CrO}_4^{2-}\), precipitating \(\text{PbCrO}_4\) under conditions of low \(\text{RSS}\). The precipitate forms slowly and consists of much larger particles.
into larger particles that are easier to filter. Surface adsorption of excess lattice ions, however, provides the precipitate's particles with a net positive or a net negative surface charge. Electrostatic repulsion between the particles prevents them from coagulating into larger particles.

Let’s use the precipitation of AgCl from a solution of AgNO₃ using NaCl as a precipitant to illustrate this effect. Early in the precipitation, when NaCl is the limiting reagent, excess Ag⁺ ions chemically adsorb to the AgCl particles, forming a positively charged primary adsorption layer (Figure 8.6a). The solution in contact with this layer contains more inert anions, NO₃⁻ in this case, than inert cations, Na⁺, giving a secondary adsorption layer with a negative charge that balances the primary adsorption layer's positive charge. The solution outside the secondary adsorption layer remains electrically neutral. Coagulation cannot occur if the secondary adsorption layer is too thick because the individual particles of AgCl are unable to approach each other closely enough.

We can induce coagulation in three ways: by decreasing the number of chemically adsorbed Ag⁺ ions, by increasing the concentration of inert ions, or by heating the solution. As we add additional NaCl, precipitating more of the excess Ag⁺, the number of chemically adsorbed silver ions decreases.
and coagulation occurs (Figure 8.6b). Adding too much NaCl, however, creates a primary adsorption layer of excess Cl\(^-\) with a loss of coagulation.

A second way to induce coagulation is to add an inert electrolyte, which increases the concentration of ions in the secondary adsorption layer. With more ions available, the thickness of the secondary absorption layer decreases. Particles of precipitate may now approach each other more closely, allowing the precipitate to coagulate. The amount of electrolyte needed to cause spontaneous coagulation is called the critical coagulation concentration.

Heating the solution and precipitate provides a third way to induce coagulation. As the temperature increases, the number of ions in the primary adsorption layer decreases, lowering the precipitate’s surface charge. In addition, heating increases the particles’ kinetic energy, allowing them to overcome the electrostatic repulsion that prevents coagulation at lower temperatures.

**Filtering the Precipitate**

After precipitating and digesting the precipitate, we separate it from solution by filtering. The most common filtration method uses filter paper, which is classified according to its speed, its size, and its ash content on ignition. Speed, or how quickly the supernatant passes through the filter paper, is a function of the paper’s pore size. A larger pore allows the supernatant to pass more quickly through the filter paper, but does not retain small particles of precipitate. Filter paper is rated as fast (retains particles larger than 20–25 \(\mu\)m), medium–fast (retains particles larger than 16 \(\mu\)m), medium (retains particles larger than 8 \(\mu\)m), and slow (retains particles larger than 2–3 \(\mu\)m). The proper choice of filtering speed is important. If the filtering speed is too fast, we may fail to retain some of the precipitate, causing a negative determinate error. On the other hand, the precipitate may clog the pores if we use a filter paper that is too slow.

Because filter paper is hygroscopic, it is not easy to dry it to a constant weight. When accuracy is important, the filter paper is removed before determining the precipitate’s mass. After transferring the precipitate and filter paper to a covered crucible, we heat the crucible to a temperature that converts the paper to CO\(_2\)(g) and H\(_2\)O(g), a process called **ignition**.

Gravity filtering is accomplished by folding the filter paper into a cone and placing it in a long-stem funnel (Figure 8.7). A seal between the filter cone and the funnel is formed by dampening the paper with water or supernatant, and pressing the paper to the wall of the funnel. When properly prepared, the funnel’s stem fills with the supernatant, increasing the rate of filtration.

The precipitate is transferred to the filter in several steps. The first step is to decant the majority of the supernatant through the filter paper without transferring the precipitate (Figure 8.8). This prevents the filter paper from clogging at the beginning of the filtration process. The precipitate is rinsed...
while it remains in its beaker, with the rinsings decanted through the filter paper. Finally, the precipitate is transferred onto the filter paper using a stream of rinse solution. Any precipitate clinging to the walls of the beaker is transferred using a rubber policeman (a flexible rubber spatula attached to the end of a glass stirring rod).

An alternative method for filtering a precipitate is a filtering crucible. The most common is a fritted-glass crucible containing a porous glass disk filter. Fritted-glass crucibles are classified by their porosity: coarse (retaining particles larger than 40–60 μm), medium (retaining particles greater than 10–15 μm), and fine (retaining particles greater than 4–5.5 μm). Another type of filtering crucible is the Gooch crucible, which is a porcelain crucible with a perforated bottom. A glass fiber mat is placed in the crucible to retain the precipitate. For both types of crucibles, the precipitate is transferred in the same manner described earlier for filter paper. Instead of using gravity, the supernatant is drawn through the crucible with the assistance of suction from a vacuum aspirator or pump (Figure 8.9).

**Rinsing the Precipitate**

Because the supernatant is rich with dissolved inert ions, we must remove any residual traces of supernatant to avoid a positive determinate error without incurring solubility losses. In many cases this simply involves the use of cold solvents or rinse solutions containing organic solvents such as ethanol. The pH of the rinse solution is critical if the precipitate contains an acidic or basic ion. When coagulation plays an important role in determining particle size, adding a volatile inert electrolyte to the rinse solution prevents the precipitate from reverting into smaller particles that might pass through the filter. This process of reverting to smaller particles is called **peptization**. The volatile electrolyte is removed when drying the precipitate.
In general, we can minimize the loss of analyte by using several small portions of rinse solution instead of a single large volume. Testing the used rinse solution for the presence of impurities is another way to guard against over rinsing the precipitate. For example, if Cl\(^-\) is a residual ion in the supernatant, we can test for its presence using AgNO\(_3\). After collecting a small portion of the rinse solution, we add a few drops of AgNO\(_3\) and look for the presence or absence of a precipitate of AgCl. If a precipitate forms, then we know that Cl\(^-\) is present and continue to rinse the precipitate. Additional rinsing is not needed if the AgNO\(_3\) does not produce a precipitate.

**Drying the Precipitate**

After separating the precipitate from its supernatant solution, the precipitate is dried to remove residual traces of rinse solution and any volatile impurities. The temperature and method of drying depend on the method of filtration and the precipitate's desired chemical form. Placing the precipitate in a laboratory oven and heating to a temperature of 110°C is sufficient when removing water and other easily volatilized impurities. Higher temperatures require a muffle furnace, a Bunsen burner, or a Meker burner, and are necessary if we need to thermally decompose the precipitate before weighing.

Because filter paper absorbs moisture, we must remove it before weighing the precipitate. This is accomplished by folding the filter paper over the precipitate and transferring both the filter paper and the precipitate to a porcelain or platinum crucible. Gentle heating first dries and then chars the filter paper. Once the paper begins to char, we slowly increase the temperature until all traces of the filter paper are gone and any remaining carbon is oxidized to CO\(_2\).
Fritted-glass crucibles can not withstand high temperatures and must be dried in an oven at temperatures below 200 °C. The glass fiber mats used in Gooch crucibles can be heated to a maximum temperature of approximately 500 °C.

**Composition of the Final Precipitate**

For a quantitative application, the final precipitate must have a well-defined composition. Precipitates containing volatile ions or substantial amounts of hydrated water, are usually dried at a temperature that completely removes these volatile species. For example, one standard gravimetric method for the determination of magnesium involves its precipitation as MgNH₄PO₄•6H₂O. Unfortunately, this precipitate is difficult to dry at lower temperatures without losing an inconsistent amount of hydrated water and ammonia. Instead, the precipitate is dried at temperatures above 1000 °C where it decomposes to magnesium pyrophosphate, Mg₂P₂O₇.

An additional problem is encountered if the isolated solid is nonstoichiometric. For example, precipitating Mn²⁺ as Mn(OH)₂ and heating frequently produces a nonstoichiometric manganese oxide, MnOₓ, where x varies between one and two. In this case the nonstoichiometric product is the result of forming of a mixture of oxides with different oxidation state of manganese. Other nonstoichiometric compounds form as a result of lattice defects in the crystal structure.

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**Representative Method 8.1**

**Determination of Mg²⁺ in Water and Wastewater**

**Description of Method**

Magnesium is precipitated as MgNH₄PO₄•6H₂O using (NH₄)₂HPO₄ as the precipitant. The precipitate's solubility in neutral solutions is relatively high (0.0065 g/100 mL in pure water at 10 °C), but it is much less soluble in the presence of dilute ammonia (0.0003 g/100 mL in 0.6 M NH₃). Because the precipitant is not selective, a preliminary separation of Mg²⁺ from potential interferents is necessary. Calcium, which is the most significant interferent, is removed by precipitating it as CaC₂O₄. The presence of excess ammonium salts from the precipitant, or the addition of too much ammonia leads to the formation of Mg(NH₄)₂(PO₄)₂, which forms Mg(PO₃)₂ after drying. The precipitate is isolated by filtering, using a rinse solution of dilute ammonia. After filtering, the precipitate is converted to Mg₂P₂O₇ and weighed.

**Procedure**

Transfer a sample containing no more than 60 mg of Mg²⁺ into a 600-mL beaker. Add 2–3 drops of methyl red indicator, and, if necessary, adjust...
the volume to 150 mL. Acidify the solution with 6 M HCl and add 10 mL of 30% w/v \((\text{NH}_4)_2\text{HPO}_4\). After cooling and with constant stirring, add concentrated NH₃ dropwise until the methyl red indicator turns yellow \((\text{pH} > 6.3)\). After stirring for 5 min, add 5 mL of concentrated NH₃ and continue stirring for an additional 10 min. Allow the resulting solution and precipitate to stand overnight. Isolate the precipitate by filtering through filter paper, rinsing with 5% v/v NH₃. Dissolve the precipitate in 50 mL of 10% v/v HCl, and precipitate a second time following the same procedure. After filtering, carefully remove the filter paper by charring. Heat the precipitate at 500 °C until the residue is white, and then bring the precipitate to constant weight at 1100 °C.

**Questions**

1. Why does the procedure call for a sample containing no more than 60 mg of Mg\(^{2+}\)?

   A 60-mg portion of Mg\(^{2+}\) generates approximately 600 mg of MgNH\(_4\)PO\(_4\)\(\cdot\)6H\(_2\)O. This is a substantial amount of precipitate. A larger quantity of precipitate may be difficult to filter and difficult to adequately rinse free of impurities.

2. Why is the solution acidified with HCl before adding the precipitant?

   The HCl ensures that MgNH\(_4\)PO\(_4\)\(\cdot\)6H\(_2\)O does not immediately precipitate when adding the precipitant. Because PO\(_4^{3-}\) is a weak base, the precipitate is soluble in a strongly acidic solution. If the precipitant is added under neutral or basic conditions (high RSS) the resulting precipitate consists of smaller, less pure particles. Increasing the pH by adding base allows the precipitate to form under more favorable (low RSS) conditions.

3. Why is the acid–base indicator methyl red added to the solution?

   The indicator's color change, which occurs at a pH of approximately 6.3, indicates when there is sufficient NH₃ to neutralize the HCl added at the beginning of the procedure. The amount of NH₃ is crucial to this procedure. If we add insufficient NH₃, then the solution is too acidic, which increases the precipitate's solubility and leads to a negative determinate error. If we add too much NH₃, the precipitate may contain traces of Mg(NH\(_4\))\(_4\)(PO\(_4\))\(_2\), which, on drying, forms Mg(PO\(_3\))\(_2\) instead of Mg\(_2\)P\(_2\)O\(_7\). This increases the mass of the ignited precipitate, giving a positive determinate error. After adding enough NH₃ to neutralize the HCl, we add the additional 5 mL of NH₃ to quantitatively precipitate MgNH\(_4\)PO\(_4\)\(\cdot\)6H\(_2\)O.

4. Explain why forming Mg(PO\(_3\))\(_2\) instead of Mg\(_2\)P\(_2\)O\(_7\) increases the precipitate's mass.
8B.2 Quantitative Applications

Although no longer a commonly used technique, precipitation gravimetry still provides a reliable means for assessing the accuracy of other methods of analysis, or for verifying the composition of standard reference materials. In this section we review the general application of precipitation gravimetry to the analysis of inorganic and organic compounds.

**Inorganic Analysis**

Table 8.1 provides a summary of some precipitation gravimetric methods for inorganic cations and anions. Several methods for the homogeneous generation of precipitants are shown in Table 8.2. The majority of inorganic precipitants show poor selectivity for the analyte. Many organic precipitants, however, are selective for one or two inorganic ions. Table 8.3 lists several common organic precipitants.

Precipitation gravimetry continues to be listed as a standard method for the determination of $\text{SO}_4^{2-}$ in water and wastewater analysis.\(^8\) Precipitation is carried out using $\text{BaCl}_2$ in an acidic solution (adjusted with $\text{HCl}$ to a pH of 4.5–5.0) to prevent the possible precipitation of $\text{BaCO}_3$ or $\text{Ba}_3(\text{PO}_4)_2$, and near the solution's boiling point. The precipitate is digested at 80–90°C for at least two hours. Ashless filter paper pulp is added to the precipitate to aid in filtration. After filtering, the precipitate is ignited to constant weight at 800°C. Alternatively, the precipitate is filtered through a fine porosity fritted glass crucible (without adding filter paper pulp), and dried to constant weight at 105°C. This procedure is subject to a variety of errors, including occlusions of $\text{Ba(NO}_3)_2$, $\text{BaCl}_2$, and alkali sulfates.

---

Several organic functional groups or heteroatoms can be determined using precipitation gravimetric methods. Table 8.4 provides a summary of several representative examples. Note that the procedure for the determination of alkoxy functional groups is an indirect analysis.

**Quantitative Calculations**

The stoichiometry of a precipitation reaction provides a mathematical relationship between the analyte and the precipitate. Because a precipitation gravimetric method may involve several chemical reactions before the precipitation reaction, knowing the stoichiometry of the precipitation reaction...
Table 8.2 Reactions for the Homogeneous Preparation of Selected Inorganic Precipitants

<table>
<thead>
<tr>
<th>Precipitant</th>
<th>Reaction</th>
</tr>
</thead>
<tbody>
<tr>
<td>OH&lt;sup&gt;−&lt;/sup&gt;</td>
<td>(NH&lt;sub&gt;2&lt;/sub&gt;)&lt;sub&gt;2&lt;/sub&gt;CO&lt;sup&gt;(aq)&lt;/sup&gt; + 3H&lt;sub&gt;2&lt;/sub&gt;O&lt;sup&gt;(l)&lt;/sup&gt; ⇌ 2NH&lt;sub&gt;4&lt;/sub&gt;&lt;sup&gt;+&lt;/sup&gt;(aq) + CO&lt;sub&gt;2&lt;/sub&gt;(g) + 2OH&lt;sup&gt;−&lt;/sup&gt;(aq)</td>
</tr>
<tr>
<td>SO&lt;sub&gt;4&lt;/sub&gt;&lt;sup&gt;2−&lt;/sup&gt;</td>
<td>NH&lt;sub&gt;2&lt;/sub&gt;HSO&lt;sub&gt;3&lt;/sub&gt;(aq) + 2H&lt;sub&gt;2&lt;/sub&gt;O(l) ⇌ NH&lt;sub&gt;4&lt;/sub&gt;&lt;sup&gt;+&lt;/sup&gt;(aq) + H&lt;sub&gt;3&lt;/sub&gt;O&lt;sup&gt;+&lt;/sup&gt;(aq) + SO&lt;sub&gt;4&lt;/sub&gt;&lt;sup&gt;2−&lt;/sup&gt;(aq)</td>
</tr>
<tr>
<td>S&lt;sup&gt;2−&lt;/sup&gt;</td>
<td>CH&lt;sub&gt;3&lt;/sub&gt;CNH&lt;sub&gt;2&lt;/sub&gt;(aq) + H&lt;sub&gt;2&lt;/sub&gt;O(l) ⇌ CH&lt;sub&gt;3&lt;/sub&gt;CN&lt;sub&gt;2&lt;/sub&gt;(aq) + H&lt;sub&gt;2&lt;/sub&gt;S(aq)</td>
</tr>
<tr>
<td>IO&lt;sub&gt;3&lt;/sub&gt;</td>
<td>HOCH&lt;sub&gt;2&lt;/sub&gt;CH&lt;sub&gt;2&lt;/sub&gt;OH(aq) + IO&lt;sub&gt;3&lt;/sub&gt;(aq) ⇌ 2HCHO(aq) + H&lt;sub&gt;2&lt;/sub&gt;O(l) + IO&lt;sub&gt;3&lt;/sub&gt;(aq)</td>
</tr>
<tr>
<td>PO&lt;sub&gt;4&lt;/sub&gt;&lt;sup&gt;3−&lt;/sup&gt;</td>
<td>(CH&lt;sub&gt;3&lt;/sub&gt;O)&lt;sub&gt;3&lt;/sub&gt;PO(aq) + 3H&lt;sub&gt;2&lt;/sub&gt;O(l) ⇌ 3CH&lt;sub&gt;3&lt;/sub&gt;OH(aq) + H&lt;sub&gt;3&lt;/sub&gt;PO&lt;sub&gt;4&lt;/sub&gt;(aq)</td>
</tr>
<tr>
<td>C&lt;sub&gt;2&lt;/sub&gt;O&lt;sub&gt;4&lt;/sub&gt;&lt;sup&gt;2−&lt;/sup&gt;</td>
<td>(C&lt;sub&gt;2&lt;/sub&gt;H&lt;sub&gt;5&lt;/sub&gt;)&lt;sub&gt;2&lt;/sub&gt;C&lt;sub&gt;2&lt;/sub&gt;O&lt;sub&gt;4&lt;/sub&gt;(aq) + 2H&lt;sub&gt;2&lt;/sub&gt;O(l) ⇌ 2C&lt;sub&gt;2&lt;/sub&gt;H&lt;sub&gt;5&lt;/sub&gt;OH(aq) + H&lt;sub&gt;2&lt;/sub&gt;C&lt;sub&gt;2&lt;/sub&gt;O&lt;sub&gt;4&lt;/sub&gt;(aq)</td>
</tr>
<tr>
<td>CO&lt;sub&gt;3&lt;/sub&gt;&lt;sup&gt;2−&lt;/sup&gt;</td>
<td>Cl&lt;sub&gt;3&lt;/sub&gt;COOH(aq) + 2OH&lt;sup&gt;−&lt;/sup&gt;(aq) ⇌ CHCl&lt;sub&gt;3&lt;/sub&gt;(aq) + CO&lt;sub&gt;3&lt;/sub&gt;&lt;sup&gt;2−&lt;/sup&gt;(aq) + H&lt;sub&gt;2&lt;/sub&gt;O(l)</td>
</tr>
</tbody>
</table>

Table 8.3 Selected Precipitation Gravimetric Methods for Inorganic Ions Using an Organic Precipitant

<table>
<thead>
<tr>
<th>Analyte</th>
<th>Precipitant</th>
<th>Structure</th>
<th>Precipitate Formed</th>
<th>Precipitate Weighed</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ni&lt;sup&gt;2+&lt;/sup&gt;</td>
<td>dimethylglyoxime</td>
<td><img src="image" alt="Dimethylglyoxime" /></td>
<td>Ni(C&lt;sub&gt;4&lt;/sub&gt;H&lt;sub&gt;7&lt;/sub&gt;O&lt;sub&gt;2&lt;/sub&gt;N&lt;sub&gt;2&lt;/sub&gt;)&lt;sub&gt;2&lt;/sub&gt;</td>
<td>Ni(C&lt;sub&gt;4&lt;/sub&gt;H&lt;sub&gt;7&lt;/sub&gt;O&lt;sub&gt;2&lt;/sub&gt;N&lt;sub&gt;2&lt;/sub&gt;)&lt;sub&gt;2&lt;/sub&gt;</td>
</tr>
<tr>
<td>Fe&lt;sup&gt;3+&lt;/sup&gt;</td>
<td>cupferron</td>
<td><img src="image" alt="Cupferron" /></td>
<td>Fe(C&lt;sub&gt;6&lt;/sub&gt;H&lt;sub&gt;5&lt;/sub&gt;N&lt;sub&gt;2&lt;/sub&gt;O&lt;sub&gt;2&lt;/sub&gt;)&lt;sub&gt;3&lt;/sub&gt;</td>
<td>Fe&lt;sub&gt;2&lt;/sub&gt;O&lt;sub&gt;3&lt;/sub&gt;</td>
</tr>
<tr>
<td>Cu&lt;sup&gt;2+&lt;/sup&gt;</td>
<td>cupron</td>
<td><img src="image" alt="Cupron" /></td>
<td>CuC&lt;sub&gt;14&lt;/sub&gt;H&lt;sub&gt;11&lt;/sub&gt;O&lt;sub&gt;2&lt;/sub&gt;N</td>
<td>CuC&lt;sub&gt;14&lt;/sub&gt;H&lt;sub&gt;11&lt;/sub&gt;O&lt;sub&gt;2&lt;/sub&gt;N</td>
</tr>
<tr>
<td>Co&lt;sup&gt;2+&lt;/sup&gt;</td>
<td>1-nitro-2-napthol</td>
<td><img src="image" alt="1-Nitro-2-Napthol" /></td>
<td>Co(C&lt;sub&gt;10&lt;/sub&gt;H&lt;sub&gt;6&lt;/sub&gt;O&lt;sub&gt;2&lt;/sub&gt;N)&lt;sub&gt;3&lt;/sub&gt;</td>
<td>Co or CoSO&lt;sub&gt;4&lt;/sub&gt;</td>
</tr>
<tr>
<td>K&lt;sup&gt;+&lt;/sup&gt;</td>
<td>sodium tetraphenylborate</td>
<td>Na[B(C&lt;sub&gt;6&lt;/sub&gt;H&lt;sub&gt;5&lt;/sub&gt;)&lt;sub&gt;4&lt;/sub&gt;]</td>
<td>K[B(C&lt;sub&gt;6&lt;/sub&gt;H&lt;sub&gt;5&lt;/sub&gt;)&lt;sub&gt;4&lt;/sub&gt;]</td>
<td></td>
</tr>
<tr>
<td>NO&lt;sub&gt;3&lt;/sub&gt;</td>
<td>nitron</td>
<td><img src="image" alt="Nitron" /></td>
<td>C&lt;sub&gt;20&lt;/sub&gt;H&lt;sub&gt;16&lt;/sub&gt;N&lt;sub&gt;4&lt;/sub&gt;HNO&lt;sub&gt;3&lt;/sub&gt;</td>
<td>C&lt;sub&gt;20&lt;/sub&gt;H&lt;sub&gt;16&lt;/sub&gt;N&lt;sub&gt;4&lt;/sub&gt;H&lt;sub&gt;2&lt;/sub&gt;NO&lt;sub&gt;3&lt;/sub&gt;</td>
</tr>
</tbody>
</table>
may not be sufficient. Even if you do not have a complete set of balanced chemical reactions, you can deduce the mathematical relationship between the analyte and the precipitate using a conservation of mass. The following example demonstrates the application of this approach to the direct analysis of a single analyte.

**Example 8.1**

To determine the amount of magnetite, Fe$_3$O$_4$, in an impure ore, a 1.5419-g sample is dissolved in concentrated HCl, giving a mixture of Fe$^{2+}$ and Fe$^{3+}$. After adding HNO$_3$ to oxidize Fe$^{2+}$ to Fe$^{3+}$ and diluting with water, Fe$^{3+}$ is precipitated as Fe(OH)$_3$ by adding NH$_3$. Filtering, rinsing, and igniting the precipitate provides 0.8525 g of pure Fe$_2$O$_3$. Calculate the %w/w Fe$_3$O$_4$ in the sample.

**Solution**

A conservation of mass requires that all the iron from the ore is found in the Fe$_2$O$_3$. We know there are 2 moles of Fe per mole of Fe$_2$O$_3$ (FW = 159.69 g/mol) and 3 moles of Fe per mole of Fe$_3$O$_4$ (FW = 231.54 g/mol); thus

$$0.8525 \text{ g Fe}_2\text{O}_3 \times \frac{2 \text{ mol Fe}}{159.69 \text{ g Fe}_2\text{O}_3} \times \frac{231.54 \text{ g Fe}_3\text{O}_4}{3 \text{ mol Fe}} = 0.82405 \text{ g Fe}_3\text{O}_4$$

The % w/w Fe$_3$O$_4$ in the sample, therefore, is

$$\frac{0.82405 \text{ g Fe}_3\text{O}_4}{1.5419 \text{ g sample}} \times 100 = 53.44\% \text{ w/w Fe}_3\text{O}_4$$
Practice Exercise 8.2

A 0.7336-g sample of an alloy containing copper and zinc is dissolved in 8 M HCl and diluted to 100 mL in a volumetric flask. In one analysis, the zinc in a 25.00-mL portion of the solution is precipitated as ZnNH$_4$PO$_4$, and subsequently isolated as Zn$_2$P$_2$O$_7$, yielding 0.1163 g. The copper in a separate 25.00-mL portion of the solution is treated to precipitate CuSCN, yielding 0.2931 g. Calculate the %w/w Zn and the %w/w Cu in the sample.

Click [here](#) to review your answer to this exercise.

In Practice Exercise 8.2 the sample contains two analytes. Because we can selectively precipitate each analyte, finding their respective concentrations is a straightforward stoichiometric calculation. But what if we cannot precipitate the two analytes separately? To find the concentrations of both analytes, we still need to generate two precipitates, at least one of which must contain both analytes. Although this complicates the calculations, we can still use a conservation of mass to solve the problem.

Example 8.2

A 0.611-g sample of an alloy containing Al and Mg is dissolved and treated to prevent interferences by the alloy’s other constituents. Aluminum and magnesium are precipitated using 8-hydroxyquinoline, providing a mixed precipitate of Al(C$_9$H$_6$NO)$_3$ and Mg(C$_9$H$_6$NO)$_2$ that weighs 7.815 g. Igniting the precipitate converts it to a mixture of Al$_2$O$_3$ and MgO that weighs 1.002 g. Calculate the %w/w Al and %w/w Mg in the alloy.

**Solution**

The masses of the solids provide us with the following two equations.

\[
g_{\text{Al(C}_9\text{H}_6\text{NO})_3} + g_{\text{Mg(C}_9\text{H}_6\text{NO})_2} = 7.815 \text{ g}
\]

\[
g_{\text{Al}_2\text{O}_3} + g_{\text{MgO}} = 1.002 \text{ g}
\]

With two equations and four unknowns, we need two additional equations to solve the problem. A conservation of mass requires that all the aluminum in Al(C$_9$H$_6$NO)$_3$ is found in Al$_2$O$_3$; thus

\[
g_{\text{Al}_2\text{O}_3} = g_{\text{Al(C}_9\text{H}_6\text{NO})_3} \times \frac{1 \text{ mol Al}}{459.45 \text{ g Al(C}_9\text{H}_6\text{NO})_3} \times \frac{101.96 \text{ g Al}_2\text{O}_3}{2 \text{ mol Al}_2\text{O}_3}
\]

\[
g_{\text{Al}_2\text{O}_3} = 0.11096 \times g_{\text{Al(C}_9\text{H}_6\text{NO})_3}
\]

Using the same approach, a conservation of mass for magnesium gives
Substituting the equations for \( g \text{MgO} \) and \( g \text{Al}_2\text{O}_3 \) into the equation for the combined weights of \( \text{MgO} \) and \( \text{Al}_2\text{O}_3 \) leaves us with two equations and two unknowns.

\[
 g \text{Al}_2\text{O}_3(\text{C}_9\text{H}_6\text{NO})_3 + g \text{Mg}_2\text{O}(\text{C}_9\text{H}_6\text{NO})_2 = 7.815 \, \text{g}
\]

\[
0.11096 \times g \text{Al}_2\text{O}_3(\text{C}_9\text{H}_6\text{NO})_3 + 0.12893 \times g \text{Mg}_2\text{O}(\text{C}_9\text{H}_6\text{NO})_2 = 1.002 \, \text{g}
\]

Multiplying the first equation by 0.11096 and subtracting the second equation gives

\[
-0.01797 \times g \text{Mg}_2\text{O}(\text{C}_9\text{H}_6\text{NO})_2 = -0.1348 \, \text{g}
\]

\[
g \text{Mg}_2\text{O}(\text{C}_9\text{H}_6\text{NO})_2 = 7.501 \, \text{g}
\]

\[
g \text{Al}_2\text{O}_3(\text{C}_9\text{H}_6\text{NO})_3 = 7.815 \, \text{g} - 7.501 \, \text{g} \text{Mg}_2\text{O}(\text{C}_9\text{H}_6\text{NO})_2 = 0.314 \, \text{g}
\]

Now we can finish the problem using the approach from Example 8.1. A conservation of mass requires that all the aluminum and magnesium in the sample of Dow metal is found in the precipitates of \( \text{Al}_2\text{O}_3(\text{C}_9\text{H}_6\text{NO})_3 \) and the \( \text{Mg}_2\text{O}(\text{C}_9\text{H}_6\text{NO})_2 \). For aluminum, we find that

\[
0.314 \, \text{g} \text{Al}_2\text{O}_3(\text{C}_9\text{H}_6\text{NO})_3 \times \frac{1 \, \text{mol Al}}{459.45 \, \text{g} \text{Al}_2\text{O}_3(\text{C}_9\text{H}_6\text{NO})_3} \times \frac{26.982 \, \text{g Al}}{\text{mol Al}} = 0.01844 \, \text{g Al}
\]

\[
\frac{0.01844 \, \text{g Al}}{0.611 \, \text{g sample}} \times 100 = 3.02\% \, \text{w/w Al}
\]

and for magnesium we have

\[
7.501 \, \text{g} \text{Mg}_2\text{O}(\text{C}_9\text{H}_6\text{NO})_2 \times \frac{1 \, \text{mol Mg}}{312.61 \, \text{g} \text{Mg}_2\text{O}(\text{C}_9\text{H}_6\text{NO})_2} \times \frac{24.305 \, \text{g Mg}}{\text{mol Mg}} = 0.5832 \, \text{g Mg}
\]

\[
\frac{0.5832 \, \text{g Mg}}{0.611 \, \text{g sample}} \times 100 = 95.5\% \, \text{w/w Mg}
\]
Although you can write the balanced reactions for any analysis, applying conservation principles can save you a significant amount of time!

Practice Exercise 8.3

A sample of a silicate rock weighing 0.8143 g is brought into solution and treated to yield a 0.2692-g mixture of NaCl and KCl. The mixture of chloride salts is subsequently dissolved in a mixture of ethanol and water, and treated with HClO₄, precipitating 0.5713 g of KClO₄. What is the %w/w Na₂O in the silicate rock?

Click here to review your answer to this exercise.

The previous problems are examples of direct methods of analysis because the precipitate contains the analyte. In an indirect analysis the precipitate forms as a result of a reaction with the analyte, but the analyte is not part of the precipitate. As shown by the following example, despite the additional complexity, we can use conservation principles to organize our calculations.

Example 8.3

An impure sample of Na₃PO₃ weighing 0.1392 g is dissolved in 25 mL of water. A solution containing 50 mL of 3% w/v HgCl₂, 20 mL of 10% w/v sodium acetate, and 5 mL of glacial acetic acid is then prepared. Adding the solution of Na₃PO₃ to the solution containing HgCl₂, oxidizes PO₃³⁻ to PO₄³⁻, precipitating Hg₂Cl₂. After digesting, filtering, and rinsing the precipitate, 0.4320 g of Hg₂Cl₂ is obtained. Report the purity of the original sample as % w/w Na₃PO₃.

Solution

This is an example of an indirect analysis because the precipitate, Hg₂Cl₂, does not contain the analyte, Na₃PO₃. Although the stoichiometry of the reaction between Na₃PO₃ and HgCl₂ is given earlier in the chapter, let’s see how we can solve the problem using conservation principles.

The reaction between Na₃PO₃ and HgCl₂ is a redox reaction in which phosphorous increases its oxidation state from +3 in Na₃PO₃ to +5 in Na₃PO₄, and in which mercury decreases its oxidation state from +2 in HgCl₂ to +1 in Hg₂Cl₂. A redox reaction must obey a conservation of electrons—all the electrons released by the reducing agent, Na₃PO₃, must be accepted by the oxidizing agent, HgCl₂. Knowing this, we write the following stoichiometric conversion factors:

\[
\frac{2 \text{ mol } e^-}{\text{mol Na}_3\text{PO}_4} \text{ and } \frac{1 \text{ mol } e^-}{\text{mol HgCl}_2}
\]

Now we are ready to solve the problem. First, we use a conservation of mass for mercury to convert the precipitate’s mass to the moles of HgCl₂.
0.4320 g Hg₂Cl₂ × \frac{2 \text{ mol Hg}}{472.09 \text{ g Hg₂Cl₂}} × \frac{1 \text{ mol HgCl₂}}{\text{mol Hg}} = 1.8302 \times 10^{-3} \text{ mol HgCl₂}

Next, we use the conservation of electrons to find the mass of Na₃PO₃.

1.8302 \times 10^{-3} \text{ mol HgCl₂} × \frac{1 \text{ mo} l e^-}{\text{mol HgCl₂}} × \frac{1 \text{ mol Na₃PO₃}}{2 \text{ mol } e^-} × \frac{147.94 \text{ g Na₃PO₃}}{\text{mol Na₃PO₃}} = 0.13538 \text{ g Na₃PO₃}

Finally, we calculate the %w/w Na₃PO₃ in the sample.

\frac{0.13538 \text{ g Na₃PO₃}}{0.1392 \text{ g sample}} \times 100 = 97.26% \text{ w/w Na₃PO₃}

**Practice Exercise 8.4**

One approach for determining phosphate, PO₄³⁻, is to precipitate it as ammonium phosphomolybdate, (NH₄)₃PO₄•12MoO₃. After isolating the precipitate by filtration, it is dissolved in acid and the molybdate precipitated and weighed as PbMoO₃. Suppose we know that our samples contain at least 12.5% Na₃PO₄ and we need to recover a minimum of 0.600 g of PbMoO₃. What is the minimum amount of sample needed for each analysis?

Click [here](#) to review your answer to this exercise.

**8B.2 Qualitative Applications**

A precipitation reaction is a useful method for identifying inorganic and organic analytes. Because a qualitative analysis does not require quantitative measurements, the analytical signal is simply the observation that a precipitate has formed. Although qualitative applications of precipitation gravimetry have been largely replaced by spectroscopic methods of analysis, they continue to find application in spot testing for the presence of specific analytes.⁹

**8B.3 Evaluating Precipitation Gravimetry**

**Scale of Operation**

The scale of operation for precipitation gravimetry is limited by the sensitivity of the balance and the availability of sample. To achieve an accuracy

---

of ±0.1% using an analytical balance with a sensitivity of ±0.1 mg, we must isolate at least 100 mg of precipitate. As a consequence, precipitation gravimetry is usually limited to major or minor analytes, in macro or meso samples (see Figure 3.5 in Chapter 3). The analysis of trace level analytes or micro samples usually requires a microanalytical balance.

**ACCURACY**

For a macro sample containing a major analyte, a relative error of 0.1–0.2% is routinely achieved. The principle limitations are solubility losses, impurities in the precipitate, and the loss of precipitate during handling. When it is difficult to obtain a precipitate that is free from impurities, it may be possible to determine an empirical relationship between the precipitate’s mass and the mass of the analyte by an appropriate calibration.

**PRECISION**

The relative precision of precipitation gravimetry depends on the sample’s size and the precipitate’s mass. For a smaller amount of sample or precipitate, a relative precision of 1–2 ppt is routinely obtained. When working with larger amounts of sample or precipitate, the relative precision can be extended to several ppm. Few quantitative techniques can achieve this level of precision.

**SENSITIVITY**

For any precipitation gravimetric method we can write the following general equation relating the signal (grams of precipitate) to the absolute amount of analyte in the sample

\[
\text{grams precipitate} = k \times \text{grams analyte}
\]

where \( k \), the method’s sensitivity, is determined by the stoichiometry between the precipitate and the analyte. Consider, for example, the determination of Fe as \( \text{Fe}_2\text{O}_3 \). Using a conservation of mass for iron, the precipitate’s mass is

\[
g_{\text{Fe}_2\text{O}_3} = g_{\text{Fe}} \times \frac{1 \text{ mol Fe}}{\text{AW Fe}} \times \frac{\text{FW Fe}_2\text{O}_3}{2 \text{ mol Fe}}
\]

and the value of \( k \) is

\[
k = \frac{1}{2} \times \frac{\text{FW Fe}_2\text{O}_3}{\text{AW Fe}}
\]

As we can see from equation 8.14, there are two ways to improve a method’s sensitivity. The most obvious way to improve sensitivity is to increase the ratio of the precipitate’s molar mass to that of the analyte. In other words, it helps to form a precipitate with the largest possible formula weight. A less obvious way to improve a method’s sensitivity is indicated by the term

Problem 8.27 provides an example of how to determine an analyte’s concentration by establishing an empirical relationship between the analyte and the precipitate.

Equation 8.13 assumes that we have used a suitable blank to correct the signal for any contributions of the reagent to the precipitate’s mass.
of 1/2 in equation 8.14, which accounts for the stoichiometry between the analyte and precipitate. We can also improve sensitivity by forming a precipitate that contains fewer units of the analyte.

**Practice Exercise 8.5**

Suppose you wish to determine the amount of iron in a sample. Which of the following compounds—FeO, Fe$_2$O$_3$, or Fe$_3$O$_4$—provides the greatest sensitivity?

Click here to review your answer to this exercise.

**Selectivity**

Due to the chemical nature of the precipitation process, precipitants are usually not selective for a single analyte. For example, silver is not a selective precipitant for chloride because it also forms precipitates with bromide and iodide. Interferents are often a serious problem and must be considered if accurate results are to be obtained.

**Time, Cost, and Equipment**

Precipitation gravimetry is time intensive and rarely practical if you have a large number of samples to analyze. However, because much of the time invested in precipitation gravimetry does not require an analyst’s immediate supervision, it may be a practical alternative when working with only a few samples. Equipment needs are few—beakers, filtering devices, ovens or burners, and balances—inexpensive, routinely available in most laboratories, and easy to maintain.

**8C Volatilization Gravimetry**

A second approach to gravimetry is to thermally or chemically decompose the sample and measure the resulting change in its mass. Alternatively, we can trap and weigh a volatile decomposition product. Because the release of a volatile species is an essential part of these methods, we classify them collectively as volatilization gravimetric methods of analysis.

**8C.1 Theory and Practice**

Whether an analysis is direct or indirect, volatilization gravimetry usually requires that we know the products of the decomposition reaction. This is rarely a problem for organic compounds, which typically decompose to form simple gases such as CO$_2$, H$_2$O, and N$_2$. For an inorganic compound, however, the products often depend on the decomposition temperature.

**Thermogravimetry**

One method for determining the products of a thermal decomposition is to monitor the sample’s mass as a function of temperature, a process called
THERMOGRAVIMETRY. Figure 8.10 shows a typical thermogram in which each change in mass—each “step” in the thermogram—represents the loss of a volatile product. As shown in Example 8.4, we can use a THERMOGRAM to identify a compound’s decomposition reactions.

Example 8.4

The thermogram in Figure 8.10 shows the mass of a sample of calcium oxalate monohydrate, CaC$_2$O$_4$•H$_2$O, as a function of temperature. The original sample weighing 17.61 mg was heated from room temperature to 1000°C at a rate of 20°C per minute. For each step in the thermogram, identify the volatilization product and the solid residue that remains.

Solution

From 100–250°C the sample loses 17.61 mg – 15.44 mg, or 2.17 mg, which is

\[
\frac{2.17\text{mg}}{17.61\text{mg}} \times 100 = 12.3\%
\]

doing the sample’s original mass. In terms of CaC$_2$O$_4$•H$_2$O, this corresponds to a loss of

\[
0.123 \times 146.11 \text{ g/mol} = 18.0 \text{ g/mol}
\]

Figure 8.10 Thermogram for CaC$_2$O$_4$•H$_2$O obtained by heating a sample from room temperature to 1000°C at a rate of 20°C/min. Each change in mass results from the loss of a volatile product. The sample’s initial mass and its mass after each loss are shown by the dotted lines. See Example 8.4 for information on interpreting this thermogram.
The product’s molar mass and the temperature range for the decomposition, suggest that this is a loss of \( \text{H}_2\text{O}(g) \), leaving a residue of \( \text{CaC}_2\text{O}_4 \).

The loss of 3.38 mg from 350–550 \( ^\circ\text{C} \) is a 19.2% decrease in the sample’s original mass, or a loss of

\[
0.192 \times 146.11 \text{ g/mol} = 28.1 \text{ g/mol}
\]

which is consistent with the loss of \( \text{CO}(g) \) and a residue of \( \text{CaCO}_3 \).

Finally, the loss of 5.30 mg from 600–800 \( ^\circ\text{C} \) is a 30.1% decrease in the sample’s original mass, or a loss of

\[
0.301 \times 146.11 \text{ g/mol} = 44.0 \text{ g/mol}
\]

This loss in molar mass is consistent with the release of \( \text{CO}_2(g) \), leaving a final residue of \( \text{CaO} \).

Identifying the products of a thermal decomposition provides information that we can use to develop an analytical procedure. For example, the thermogram in Figure 8.1 shows that we must heat a precipitate of \( \text{CaC}_2\text{O}_4\cdot\text{H}_2\text{O} \) to a temperature between 250 and 400 \( ^\circ\text{C} \) if we wish to isolate and weigh \( \text{CaC}_2\text{O}_4 \). Alternatively, heating the sample to 1000 \( ^\circ\text{C} \) allows us to isolate and weigh \( \text{CaO} \).

### Practice Exercise 8.6

Under the same conditions as Figure 8.1, the thermogram for a 22.16 mg sample of \( \text{MgC}_2\text{O}_4\cdot\text{H}_2\text{O} \) shows two steps: a loss of 3.06 mg from 100–250 \( ^\circ\text{C} \) and a loss of 12.24 mg from 350–550 \( ^\circ\text{C} \). For each step, identify the volatilization product and the solid residue that remains.

Using your results from this exercise and the results from Example 8.4, explain how you can use thermogravimetry to analyze a mixture containing \( \text{CaC}_2\text{O}_4\cdot\text{H}_2\text{O} \) and \( \text{MgC}_2\text{O}_4\cdot\text{H}_2\text{O} \). You may assume that other components in the sample are inert and thermally stable below 1000 \( ^\circ\text{C} \).

Click [here](#) to review your answer to this exercise.

### Equipment

Depending on the method of analysis, the equipment for volatilization gravimetry may be simple or complex. In the simplest experimental design, we place the sample in a crucible and decompose it at a fixed temperature using a Bunsen burner, a Meker burner, a laboratory oven, or a muffle furnace. The sample’s mass and the mass of the residue are measured using an analytical balance.

Trapping and weighing the volatile products of a thermal decomposition requires specialized equipment. The sample is placed in a closed container and heated. As decomposition occurs, a stream of an inert purge-gas sweeps the volatile products through one or more selective absorbent traps.
In a thermogravimetric analysis, the sample is placed on a small balance pan attached to one arm of an electromagnetic balance (Figure 8.11). The balance sits on the top of the instrument with the sample suspended below. A gas line supplies an inert gas that sweeps the volatile decomposition products out of the furnace. The heat exchanger dissipates the heat from the furnace to a reservoir of water. (b) Close-up showing the balance pan, which sits on a moving platform, the thermocouple for monitoring temperature, a hook for lowering the sample pan into the furnace, and the opening to the furnace. After placing a small portion of the sample on the balance pan, the platform rotates over the furnace and transfers the balance pan to a hook that is suspended from the balance. Once the balance pan is in place, the platform rotates back to its initial position. The balance pan and the thermocouple are then lowered into the furnace.

The best way to appreciate the theoretical and practical details discussed in this section is to carefully examine a typical volatilization gravimetric method. Although each method is unique, the determination of Si in ores and alloys by forming volatile SiF₄ provides an instructive example of a typical procedure. The description here is based on a procedure from Young, R. S. Chemical Analysis in Extractive Metallurgy, Griffen: London, 1971, pp. 302–304.

In a thermogravimetric analysis, the sample is placed on a small balance pan attached to one arm of an electromagnetic balance (Figure 8.11). The sample is lowered into an electric furnace and the furnace’s temperature is increased at a fixed rate of few degrees per minute while continuously monitoring the sample’s weight. The instrument usually includes a gas line for purging the volatile decomposition products out of the furnace, and a heat exchanger to dissipate the heat emitted by the furnace.

**Representative Method 8.2**

**Determination of Si in Ores and Alloys**

**Description of Method**

Silicon is determined by dissolving the sample in acid and dehydrating to precipitate SiO₂. Because a variety of other insoluble oxides also form, the precipitate’s mass is not a direct measure of the amount of silicon in the sample. Treating the solid residue with HF results in the formation of volatile SiF₄. The decrease in mass following the loss of SiF₄ provides an indirect measure of the amount of silicon in the original sample.

**Procedure**

Transfer a sample of between 0.5 and 5.0 g to a platinum crucible along with an excess of Na₂CO₃, and heat until a melt forms. After cooling,
dissolve the residue in dilute HCl. Evaporate the solution to dryness on a steam bath and heat the residue, which contains SiO₂ and other solids, for one hour at 110°C. Moisten the residue with HCl and repeat the dehydration. Remove any acid soluble materials from the residue by adding 50 mL of water and 5 mL of concentrated HCl. Bring the solution to a boil and filter through #40 filter paper. Wash the residue with hot 2% v/v HCl followed by hot water. Evaporate the filtrate to dryness twice and, following the same procedure, treat to remove any acid-soluble materials. Combine the two precipitates, and dry and ignite to a constant weight at 1200°C. After cooling, add 2 drops of 50% v/v H₂SO₄ and 10 mL of HF. Remove the volatile SiF₄ by evaporating to dryness on a hot plate. Finally, bring the residue to constant weight by igniting at 1200°C.

**Questions**

1. According to the procedure the sample should weigh between 0.5 and 5.0 g. How should you decide upon the amount of sample to use?  
   In this procedure the critical measurement is the decrease in mass following the volatilization of SiF₄. The reaction responsible for the loss of mass is

   \[
   \text{SiO}_2(s) + 4\text{HF}(aq) \rightarrow \text{SiF}_4(g) + 2\text{H}_2\text{O}(l)
   \]

   Water and any excess HF are removed during the final ignition, and do not contribute to the change in mass. The loss in mass, therefore, is equivalent to the mass of SiO₂ present after the dehydration step. Every 0.1 g of Si in the original sample results in the loss of 0.21 g of SiO₂.

   How much sample we use depends on what is an acceptable uncertainty when measuring mass. A 0.5-g sample that is 50% w/w in Si, for example, will lose 0.53 g. If we are using a balance that measures mass to the nearest ±0.1 mg, then the relative uncertainty in mass is approximately ±0.02%; this is a reasonable level of uncertainty for a gravimetric analysis. A 0.5 g sample that is only 5% w/w Si experiences a weight loss of only 0.053 g and has a relative uncertainty of ±0.2%. In this case a larger sample is needed.

2. Why are acid-soluble materials removed before treating the dehydrated residue with HF?  
   Any acid-soluble materials in the sample will react with HF or H₂SO₄. If the products of these reactions are volatile, or if they decompose at 1200°C, then the change in mass is not due solely to the volatilization of SiF₄. As a result, we overestimate the amount of Si in our sample.
8C.2 Quantitative Applications

Unlike precipitation gravimetry, which is rarely used as a standard method of analysis, volatilization gravimetric methods continue to play an important role in chemical analysis. Several important examples are discussed below.

**Inorganic Analysis**

Determining the inorganic ash content of an organic material, such as a polymer, is an example of a direct volatilization gravimetric analysis. After weighing the sample, it is placed in an appropriate crucible and the organic material carefully removed by combustion, leaving behind the inorganic ash. The crucible containing the residue is heated to a constant weight using either a burner or an oven before determining the mass of the inorganic ash.

Another example of volatilization gravimetry is the determination of dissolved solids in natural waters and wastewaters. In this method, a sample of water is transferred to a weighing dish and dried to a constant weight at either 103–105 °C or at 180 °C. Samples dried at the lower temperature retain some occluded water and lose some carbonate as CO$_2$. The loss of organic material, however, is minimal. At the higher temperature, the residue is free from occluded water, but the loss of carbonate is greater. In addition, some chloride, nitrate, and organic material is lost through thermal decomposition. In either case, the residue that remains after drying to a constant weight at 500 °C is the amount of fixed solids in the sample, and the loss in mass provides an indirect measure of the sample’s volatile solids.

Indirect analyses based on the weight of residue remaining after volatilization are commonly used in determining moisture in a variety of products, and in determining silica in waters, wastewaters, and rocks. Moisture is determined by drying a preweighed sample with an infrared lamp or a low temperature oven. The difference between the original weight and the weight after drying equals the mass of water lost.

3. Why is H$_2$SO$_4$ added with the HF?

Many samples containing silicon also contain aluminum and iron, which, when dehydrating the sample, form Al$_2$O$_3$ and Fe$_2$O$_3$. These oxides are potential interferents because they also form volatile fluorides. In the presence of H$_2$SO$_4$, however, aluminum and iron preferentially form non-volatile sulfates. These sulfates eventually decompose back to their respective oxides when we heat the residue to 1200 °C. As a result, the change in weight after treating with HF and H$_2$SO$_4$ is due only to the loss of SiF$_4$. 


Organic Analysis

The most important application of volatilization gravimetry is for the elemental analysis of organic materials. During combustion with pure O₂, many elements, such as carbon and hydrogen, are released as gaseous combustion products, such as CO₂(g) and H₂O(g). Passing the combustion products through preweighed tubes containing selective absorbents and measuring the increases in mass provides a direct analysis for the mass of carbon and hydrogen in the organic material.

Alkaline metals and earths in organic materials can be determined by adding H₂SO₄ to the sample before combustion. After combustion is complete, the metal remains behind as a solid residue of metal sulfate. Silver, gold, and platinum can be determined by burning the organic sample, leaving a metallic residue of Ag, Au, or Pt. Other metals are determined by adding HNO₃ before combustion, leaving a residue of the metal oxide.

Volatileization gravimetry is also used to determine biomass in waters and wastewaters. Biomass is a water quality index that provides an indication of the total mass of organisms contained within a sample of water. A known volume of the sample is passed through a preweighed 0.45-μm membrane filter or a glass-fiber filter, and dried at 105°C for 24 h. The residue's mass provides a direct measure of biomass. If samples are known to contain a substantial amount of dissolved inorganic solids, the residue can be ignited at 500°C for one hour, volatilizing the biomass. The resulting inorganic residue is wetted with distilled water to rehydrate any clay minerals and dried to a constant weight at 105°C. The difference in mass before and after ignition provides an indirect measure of biomass.

Quantitative Calculations

For some applications, such as determining the amount of inorganic ash in a polymer, a quantitative calculation is straightforward and does not require a balanced chemical reaction. For other applications, however, the relationship between the analyte and the analytical signal depends upon the stoichiometry of any relevant reactions. Once again, a conservation of mass is useful when solving problems.

Example 8.5

A 101.3-mg sample of an organic compound containing chlorine is combusted in pure O₂ and the volatile gases collected in absorbent traps. The trap for CO₂ increases in mass by 167.6 mg and the trap for H₂O shows a 13.7-mg increase. A second sample of 121.8 mg is treated with concentrated HNO₃ producing Cl₂, which subsequently reacts with Ag⁺, forming 262.7 mg of AgCl. Determine the compound’s composition, as well as its empirical formula.
A conservation of mass requires that all the carbon in the organic compound must be in the CO\textsubscript{2} produced during combustion; thus

\[
167.6 \text{ mg CO}_2 \times \frac{1 \text{ g CO}_2}{1000 \text{ mg CO}_2} \times \frac{1 \text{ mol C}}{44.011 \text{ g CO}_2} \times \frac{12.011 \text{ g C}}{\text{mol C}} \times \frac{1000 \text{ mg C}}{\text{g C}} = 45.74 \text{ mg C}
\]

\[
\frac{45.74 \text{ mg C}}{101.3 \text{ mg sample}} \times 100 = 45.15\% \text{ w/w C}
\]

Using the same approach for hydrogen and chlorine, we find that

\[
13.7 \text{ mg H}_2\text{O} \times \frac{1 \text{ g H}_2\text{O}}{1000 \text{ mg H}_2\text{O}} \times \frac{2 \text{ mol H}}{18.015 \text{ g H}_2\text{O}} \times \frac{1.008 \text{ g H}}{\text{mol H}} \times \frac{1000 \text{ mg H}}{\text{g H}} = 1.533 \text{ mg H}
\]

\[
\frac{1.533 \text{ mg H}}{101.3 \text{ mg sample}} \times 100 = 1.51\% \text{ w/w H}
\]

\[
262.7 \text{ mg AgCl} \times \frac{1 \text{ g AgCl}}{1000 \text{ mg AgCl}} \times \frac{1 \text{ mol Cl}}{143.32 \text{ g AgCl}} \times \frac{35.453 \text{ g Cl}}{\text{mol Cl}} \times \frac{1000 \text{ mg Cl}}{\text{g Cl}} = 64.98 \text{ mg Cl}
\]

\[
\frac{64.98 \text{ mg Cl}}{121.8 \text{ mg sample}} \times 100 = 53.35\% \text{ w/w Cl}
\]

Adding together the weight percents for C, H, and Cl gives a total of 100.01%; thus, the compound contains only these three elements. To determine the compound’s empirical formula we note that a gram of sample contains 0.4515 g of C, 0.0151 g of H and 0.5335 g of Cl. Expressing each element in moles gives 0.0376 moles C, 0.0150 moles H and 0.0150 moles Cl. Hydrogen and chlorine are present in a 1:1 molar ratio. The molar ratio of C to moles of H or Cl is

\[
\frac{\text{moles C}}{\text{moles H}} = \frac{\text{moles C}}{\text{moles Cl}} = \frac{0.0376}{0.0150} = 2.51 \approx 2.5
\]

Thus, the simplest, or empirical formula for the compound is $C_5H_2Cl_2$. 

\[\text{ Solution}\]
In an indirect volatilization gravimetric analysis, the change in the sample's weight is proportional to the amount of analyte. Note that in the following example it is not necessary to apply a conservation of mass to relate the analytical signal to the analyte.

**Example 8.6**

A sample of slag from a blast furnace is analyzed for SiO\textsubscript{2} by decomposing a 0.5003-g sample with HCl, leaving a residue with a mass of 0.1414 g. After treating with HF and H\textsubscript{2}SO\textsubscript{4}, and evaporating the volatile SiF\textsubscript{4}, a residue with a mass of 0.0183 g remains. Determine the %w/w SiO\textsubscript{2} in the sample.

**Solution**

In this procedure the difference in the residue's mass before and after volatilizing SiF\textsubscript{4} gives the mass of SiO\textsubscript{2} in the sample; thus the sample contains

\[
0.1414 \text{ g} - 0.0183 \text{ g} = 0.1231 \text{ g SiO}_2
\]

and the %w/w SiO\textsubscript{2} is

\[
\frac{0.1231 \text{ g SiO}_2}{0.5003 \text{ g}} \times 100 = 24.61\% \text{ w/w SiO}_2
\]

**Practice Exercise 8.7**

Heating a 0.3317-g mixture of CaC\textsubscript{2}O\textsubscript{4} and MgC\textsubscript{2}O\textsubscript{4} yields a residue of 0.1794 g at 600 °C and a residue of 0.1294 g at 1000 °C. Calculate the %w/w CaC\textsubscript{2}O\textsubscript{4} in the sample. You may wish to review your answer to **Practice Exercise 8.6** as you consider this problem.

Click [here](#) to review your answer to this exercise.

Finally, in some quantitative applications we can compare the result for a sample to a similar result obtained using a standard.

**Example 8.7**

A 26.23-mg sample of MgC\textsubscript{2}O\textsubscript{4}•H\textsubscript{2}O and inert materials is heated to constant weight at 1200 °C, leaving a residue weighing 20.98 mg. A sample of pure MgC\textsubscript{2}O\textsubscript{4}•H\textsubscript{2}O, when treated in the same fashion, undergoes a 69.08% change in its mass. Determine the %w/w MgC\textsubscript{2}O\textsubscript{4}•H\textsubscript{2}O in the sample.

**Solution**

The change in the sample's mass is 5.25 mg, which corresponds to
Alternatively, you can determine that the final product of the decomposition is MgO (see Practice Exercise 8.6) and use a conservation of mass for Mg to arrive at the same answer.

\[
5.25 \text{ mg lost} \times \frac{100.0 \text{ mg MgC}_2\text{O}_4 \cdot \text{H}_2\text{O}}{69.08 \text{ mg lost}} = 7.60 \text{ mg MgC}_2\text{O}_4 \cdot \text{H}_2\text{O}
\]

The %w/w MgC\(_2\)O\(_4\)•H\(_2\)O in the sample is

\[
\frac{7.60 \text{ mg MgC}_2\text{O}_4 \cdot \text{H}_2\text{O}}{26.23 \text{ mg sample}} \times 100 = 29.0 \% \text{ w/w MgC}_2\text{O}_4 \cdot \text{H}_2\text{O}
\]

### 8C.3 Evaluating Volatilization Gravimetry

The scale of operation, accuracy, and precision of a gravimetric volatilization method is similar to that described in Section 8B.4 for precipitation gravimetry. The sensitivity of a direct analysis is fixed by the analyte's chemical form following combustion or volatilization. We can improve the sensitivity of an indirect analysis by choosing conditions that give the largest possible change in mass. For example, the thermogram in Figure 8.10 shows us that an indirect analysis for CaC\(_2\)O\(_4\)•H\(_2\)O is more sensitive if we measure the change in mass following ignition at 1000°C than if we ignite the sample at 300°C.

Selectivity is not a problem for a direct analysis if we trap the analyte using a selective absorbent trap. A direct analysis based on the residue's weight following combustion or volatilization is possible if the residue only contains the analyte of interest. As noted earlier, an indirect analysis is only feasible when the change in mass results from the loss of a single volatile product containing the analyte.

Volatilization gravimetric methods are time and labor intensive. Equipment needs are few, except when combustion gases must be trapped, or for a thermogravimetric analysis, when specialized instrumentation is needed.

### 8D Particulate Gravimetry

Precipitation and volatilization gravimetric methods require that the analyte, or some other species in the sample, participate in a chemical reaction. In a direct precipitation gravimetric analysis, for example, we convert a soluble analyte into an insoluble form that precipitates from solution. In some situations, however, the analyte is already present as in a particulate form that is easy to separate from its liquid, gas, or solid matrix. When such a separation is possible, we can determine the analyte’s mass without relying on a chemical reaction.

#### 8D.1 Theory and Practice

There are two methods for separating a particulate analyte from its matrix. The most common method is filtration, in which we separate solid par-
ticulates from their gas, liquid, or solid matrix. A second method, which is useful for gas particles, solutes, and solids, is an extraction.

**Filtration**

To separate solid particulates from their matrix we use gravity or apply suction from a vacuum pump or aspirator to pull the sample through a filter. The type of filter we use depends upon the size of the solid particles and the sample's matrix. Filters for liquid samples are constructed from a variety of materials, including cellulose fibers, glass fibers, cellulose nitrate, and polytetrafluoroethylene (PTFE). Particle retention depends on the size of the filter’s pores. Cellulose fiber filter papers range in pore size from 30 μm to 2–3 μm. Glass fiber filters, manufactured using chemically inert borosilicate glass, are available with pore sizes between 2.5 μm and 0.3 μm. Membrane filters, which are made from a variety of materials, including cellulose nitrate and PTFE, are available with pore sizes from 5.0 μm to 0.1 μm.

Solid aerosol particulates are collected using either a single-stage or a multiple-stage filter. In a single-stage system, we pull the gas through a single filter, retaining particles larger than the filter’s pore size. When collecting samples from a gas line, we place the filter directly in the line. Atmospheric gases are sampled with a high volume sampler that uses a vacuum pump to pull air through the filter at a rate of approximately 75 m³/h. In either case, the filtering media for liquid samples also can be used to collect aerosol particulates. In a multiple-stage system, a series of filtering units separates the particulates into several narrow size ranges.

The particulates in a solid matrix are separated by size using one or more sieves (Figure 8.12). Sieves are available in a variety of mesh sizes ranging from approximately 25 mm to 40 μm. By stacking sieves of different mesh size, we can isolate particulates into several narrow size ranges. Using the sieves in Figure 8.12, for example, we can separate a solid into particles with diameters >1700 μm, with diameters between 1700 μm and 500 μm, with diameters between 500 μm and 250μm, and those with a diameter <250 μm.

**Extraction**

Filtering limits particulate gravimetry to solid analytes that are easily separated from their matrix. We can extend particulate gravimetry to the analysis of gas phase analytes, solutes, and poorly filterable solids by extracting them with a suitable solvent. After the extraction, we evaporate the solvent before determining the analyte’s mass. Alternatively, we can determine the analyte indirectly by measuring the change in the sample’s mass after extracting the analyte. Solid-phase extractions, such as those described in Chapter 7, also may be used.
Another method for extracting an analyte from its matrix is by adsorption onto a solid substrate, by absorption into a thin polymer or chemical film coated on a solid substrate, or by chemically binding to a suitable receptor that is covalently bound to a solid substrate (Figure 8.13). Adsorption, absorption, and binding occur at the interface between the solution containing the analyte and the substrate’s surface, the thin film, or the receptor. Although the amount of extracted analyte is too small to measure using a conventional balance, it can be measured using a quartz crystal microbalance.

The measurement of mass using a quartz crystal microbalance takes advantage of the piezoelectric effect. The application of an alternating electrical field across a quartz crystal induces an oscillatory vibrational motion in the crystal. Every quartz crystal vibrates at a characteristic resonant frequency that depends on the crystal’s properties, including the mass per unit area of any material coated on the crystal’s surface. The change in mass following adsorption, absorption, or binding of the analyte, therefore, can be determined by monitoring the change in the quartz crystal’s characteristic resonant frequency. The exact relationship between the change in frequency and mass is determined by a calibration curve.

8D.2 Quantitative Applications

Particulate gravimetry is important in the environmental analysis of water, air, and soil samples. The analysis for suspended solids in water samples, for example, is accomplished by filtering an appropriate volume of a well-

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mixed sample through a glass fiber filter and drying the filter to constant weight at 103–105°C.

The microbiological testing of water also uses particulate gravimetry. One example is the analysis for coliform bacteria in which an appropriate volume of sample is passed through a sterilized 0.45-μm membrane filter. The filter is placed on a sterilized absorbent pad saturated with a culturing medium and incubated for 22–24 hours at 35 ± 0.5°C. Coliform bacteria are identified by the presence of individual bacterial colonies that form during the incubation period (Figure 8.14). As with qualitative applications of precipitation gravimetry, the signal in this case is a visual observation rather than a measurement of mass.

Total airborne particulates are determined using a high-volume air sampler equipped with either cellulose fiber or glass fiber filters. Samples from urban environments require approximately 1 h of sampling time, but samples from rural environments require substantially longer times.

Grain size distributions for sediments and soils are used to determine the amount of sand, silt, and clay in a sample. For example, a grain size of 2 mm serves as the boundary between gravel and sand. The grain size for the sand–silt and the silt–clay boundaries are 1/16 mm and 1/256 mm, respectively.

Several standard quantitative analytical methods for agricultural products are based on measuring the sample’s mass following a selective solvent extraction. For example, the crude fat content in chocolate can be determined by extracting with ether for 16 hours in a Soxhlet extractor. After the extraction is complete, the ether is allowed to evaporate and the residue is weighed after drying at 100°C. This analysis has also been accomplished indirectly by weighing a sample before and after extracting with supercritical CO₂.

Quartz crystal microbalances equipped with thin film polymer films or chemical coatings have found numerous quantitative applications in environmental analysis. Methods have been reported for the analysis of a variety of gaseous pollutants, including ammonia, hydrogen sulfide, ozone, sulfur dioxide, and mercury. Biochemical particulate gravimetric sensors also have been developed. For example, a piezoelectric immunosensor has been developed that shows a high selectivity for human serum albumin, and is capable of detecting microgram quantities.¹¹

**Quantitative Calculations**

The result of a quantitative analysis by particulate gravimetry is just the ratio, using appropriate units, of the amount of analyte relative to the amount of sample.

Example 8.8

A 200.0-mL sample of water was filtered through a pre-weighed glass fiber filter. After drying to constant weight at 105 °C, the filter was found to have increased in mass by 48.2 mg. Determine the sample’s total suspended solids.

Solution

A ppm is equivalent to a mg of analyte per liter of solution; thus, the total suspended solids for the sample is

\[
\frac{48.2 \text{ mg solids}}{0.2000 \text{ L sample}} = 241 \text{ ppm solids}
\]

8D.3 Evaluating Particulate Gravimetry

The scale of operation and detection limit for particulate gravimetry can be extended beyond that of other gravimetric methods by increasing the size of the sample taken for analysis. This is usually impracticable for other gravimetric methods because of the difficulty of manipulating a larger sample through the individual steps of the analysis. With particulate gravimetry, however, the part of the sample that is not analyte is removed when filtering or extracting. Consequently, particulate gravimetry is easily extended to the analysis of trace-level analytes.

Except for methods relying on a quartz crystal microbalance, particulate gravimetry uses the same balances as other gravimetric methods, and is capable of achieving similar levels of accuracy and precision. Since particulate gravimetry is defined in terms of the mass of the particle itself, the sensitivity of the analysis is given by the balance’s sensitivity. Selectivity, on the other hand, is determined either by the filter’s pore size, or by the properties of the extracting phase. Because it requires a single step, particulate gravimetric methods based on filtration generally require less time, labor and capital than other gravimetric methods.

8E Key Terms

- coagulation
- definitive technique
- electrogravimetry
- ignition
- occlusion
- precipitant
- relative supersaturation
- surface adsorbate
- volatilization gravimetry
- conservation of mass
- coprecipitate
- digestion
- direct analysis
- gravimetry
- homogeneous precipitation
- inclusion
- indirect analysis
- particulate gravimetry
- peptization
- precipitation gravimetry
- reprecipitation
- thermogram
- quartz crystal microbalance
- supernatant
- thermogravimetry
8F Chapter Summary

In a gravimetric analysis, a measurement of mass or a change in mass provides quantitative information about the analyte. The most common form of gravimetry uses a precipitation reaction to generate a product whose mass is proportional to the amount of analyte. In many cases the precipitate includes the analyte; however, an indirect analysis in which the analyte causes the precipitation of another compound also is possible. Precipitation gravimetric procedures must be carefully controlled to produce precipitates that are easy to filter, free from impurities, and of known stoichiometry.

In volatilization gravimetry, thermal or chemical energy decomposes the sample containing the analyte. The mass of residue remaining after decomposition, the mass of volatile products collected with a suitable trap, or a change in mass due to the loss of volatile material are all gravimetric measurements.

When the analyte is already present in a particulate form that is easy to separate from its matrix, then a particulate gravimetric analysis may be feasible. Examples include the determination of dissolved solids and the determination of fat in foods.

8G Problems

1. Starting with the equilibrium constant expressions for reaction 8.1, and reactions 8.3–8.5, verify that equation 8.7 is correct.

2. Equation 8.7 explains how the solubility of AgCl varies as a function of the equilibrium concentration of Cl\(^{-}\). Derive a similar equation that describes the solubility of AgCl as a function of the equilibrium concentration of Ag\(^{+}\). Graph the resulting solubility function and compare it to that shown in Figure 8.1.

3. Construct a solubility diagram for Zn(OH)\(_2\) that takes into account the following soluble zinc-hydroxide complexes: Zn(OH)\(^+\), Zn(OH)\(_3\)\(^-\), and Zn(OH)\(_4\)\(^2-\). What is the optimum pH for quantitatively precipitating Zn(OH)\(_2\)? For your solubility diagram, plot \(\log(S)\) on the y-axis and pH on the x-axis. See the appendices for relevant equilibrium constants.

4. Starting with equation 8.10, verify that equation 8.11 is correct.

5. For each of the following precipitates, use a ladder diagram to identify the pH range where the precipitates has its lowest solubility? See the appendices for relevant equilibrium constants.
   a. CaC\(_2\)O\(_4\)  b. PbCrO\(_4\)  c. BaSO\(_4\)
   d. SrCO\(_3\)  e. ZnS
6. Mixing solutions of 1.5 M KNO₃ and 1.5 M HClO₄ produces a white precipitate of KClO₄. If permanganate ions are present, an inclusion of KMnO₄ is possible. Impure precipitates of KClO₄ are purple if an inclusion of KMnO₄ is present. Shown below are descriptions of two experiments in which KClO₄ is precipitated in the presence of MnO₄⁻. Explain why the experiments lead to the different results shown in Figure 8.15.

**Experiment 1.** Place 1 mL of 1.5 M KNO₃ in a test tube, add 3 drops of 0.1 M KMnO₄, and swirl to mix. Add 1 mL of 1.5 M HClO₄ dropwise, agitating the solution between drops. Destroy the excess KMnO₄ by adding 0.1 M NaHSO₃ dropwise. The resulting precipitate of KClO₄ has an intense purple color.

**Experiment 2.** Place 1 mL of 1.5 M HClO₄ in a test tube, add 3 drops of 0.1 M KMnO₄, and swirl to mix. Add 1 mL of 1.5 M KNO₃ dropwise, agitating the solution between drops. Destroy the excess KMnO₄ by adding 0.1 M NaHSO₃ dropwise. The resulting precipitate of KClO₄ has a pale purple in color.

7. Mixing solutions of Ba(SCN)₂ and MgSO₄ produces a precipitate of BaSO₄. Shown below are the descriptions and results for three experiments using different concentrations of Ba(SCN)₂ and MgSO₄. Explain why these experiments produce different results.

**Experiment 1.** When equal volumes of 3.5 M Ba(SCN)₂ and 3.5 M MgSO₄ are mixed, a gelatinous precipitate immediately forms.

**Experiment 2.** When equal volumes of 1.5 M Ba(SCN)₂ and 1.5 M MgSO₄ are mixed, a curdy precipitate immediately forms. Individual particles of BaSO₄ can be seen as points under a magnification of 1500× (a particle size less than 0.2 μm).

**Experiment 3.** When equal volumes of 0.5 mM Ba(SCN)₂ and 0.5 mM MgSO₄ are mixed, the complete precipitation of BaSO₄ requires 2–3 h. Individual crystals of BaSO₄ obtain lengths of approximately 5 μm.

8. Aluminum is determined gravimetrically by precipitating Al(OH)₃ and isolating Al₂O₃. A sample containing approximately 0.1 grams of Al is dissolved in 200 mL of H₂O, and 5 grams of NH₄Cl and a few drops of methyl red indicator are added (methyl red is red at pH levels below 4 and yellow at pH levels above 6). The solution is heated to boiling and 1:1 NH₃ is added dropwise till the indicator turns yellow, precipitating Al(OH)₃. The precipitate is held at the solution's boiling point for several minutes before filtering and rinsing with a hot solution of 2% w/v NH₄NO₃. The precipitate is then ignited at 1000–1100 °C, forming Al₂O₃.
(a) Cite two ways in which this procedure encourages the formation of larger particles of precipitate.

(b) The ignition step must be carried out carefully to ensure the quantitative conversion of Al(OH)$_3$ to Al$_2$O$_3$. What is the effect of an incomplete conversion on the %w/w Al?

(c) What is the purpose of adding NH$_4$Cl and methyl red indicator?

(d) An alternative procedure involves isolating and weighing the precipitate as the 8-hydroxyquinolate, Al(C$_9$H$_6$ON)$_3$. Why might this be a more advantageous form of Al for a gravimetric analysis? Are there any disadvantages?

9. Calcium is determined gravimetrically by precipitating CaC$_2$O$_4\cdot$H$_2$O and isolating CaCO$_3$. After dissolving a sample in 10 mL of water and 15 mL of 6 M HCl, the resulting solution is heated to boiling and a warm solution of excess ammonium oxalate is added. The solution is maintained at 80°C and 6 M NH$_3$ is added dropwise, with stirring, until the solution is faintly alkaline. The resulting precipitate and solution are removed from the heat and allowed to stand for at least one hour. After testing the solution for completeness of precipitation, the sample is filtered, rinsed with 0.1% w/v ammonium oxalate, and dried at 100–120°C for 1 hour. The precipitate is transferred to a muffle furnace where it is converted to CaCO$_3$ by drying at 500 ± 25°C until constant weight.

(a) Why is the precipitate of CaC$_2$O$_4\cdot$H$_2$O converted to CaCO$_3$?

(b) In the final step, if the sample is heated at too high of a temperature some CaCO$_3$ may be converted to CaO. What effect would this have on the reported %w/w Ca?

(c) Why is the precipitant, (NH$_4$)$_2$C$_2$O$_4$, added to a hot, acidic solution instead of a cold, alkaline solution?

10. Iron is determined gravimetrically by precipitating as Fe(OH)$_3$ and igniting to Fe$_2$O$_3$. After dissolving a sample in 50 mL of H$_2$O and 10 mL of 6 M HCl, any Fe$^{2+}$ is converted Fe$^{3+}$ by oxidizing with 1–2 mL of concentrated HNO$_3$. The sample is heated to remove the oxides of nitrogen and the solution is diluted to 200 mL. After bringing the solution to a boil, Fe(OH)$_3$ is precipitated by slowly adding 1:1 NH$_3$ until the odor of NH$_3$ is detected. The solution is boiled for an additional minute and the precipitate is allowed to settle. The precipitate is then filtered and rinsed with several portions of hot 1% w/v NH$_4$NO$_3$ until no Cl$^-$ is found in the wash water. Finally, the precipitate is ignited to constant weight at 500–550°C and weighed as Fe$_2$O$_3$. 
(a) If ignition is not carried out under oxidizing conditions (plenty of \(O_2\) present), the final product may contain \(Fe_3O_4\). What effect would this have on the reported %w/w Fe?

(b) The precipitate is washed with a dilute solution of \(NH_4NO_3\). Why is \(NH_4NO_3\) added to the wash water?

(c) Why does the procedure call for adding \(NH_3\) until the odor of ammonia is detected?

(d) Describe how you might test the filtrate for Cl\(^-\).

11. Sinha and Shome described a gravimetric method for molybdenum in which it is precipitated as \(MoO_2(C_{13}H_{10}NO_2)_2\) using \(\mu\)-benzoylphenylhydroxylamine, \(C_{13}H_{11}NO_2\), as a precipitant.\(^{12}\) The precipitate is weighed after igniting to \(MoO_3\). As part of their study, the authors determined the optimum conditions for the analysis. Samples containing 0.0770 g of Mo were taken through the procedure while varying the temperature, the amount of precipitant added, and the pH of the solution. The solution volume was held constant at 300 mL for all experiments. A summary of their results are shown in the following table.

<table>
<thead>
<tr>
<th>Temperature (^{\circ})C</th>
<th>Mass (g) of precipitant</th>
<th>Volume (mL) of 10 M HCl</th>
<th>Mass (g) of (MoO_3)</th>
</tr>
</thead>
<tbody>
<tr>
<td>30</td>
<td>0.20</td>
<td>0.9</td>
<td>0.0675</td>
</tr>
<tr>
<td>30</td>
<td>0.30</td>
<td>0.9</td>
<td>0.1014</td>
</tr>
<tr>
<td>30</td>
<td>0.35</td>
<td>0.9</td>
<td>0.1140</td>
</tr>
<tr>
<td>30</td>
<td>0.42</td>
<td>0.9</td>
<td>0.1155</td>
</tr>
<tr>
<td>30</td>
<td>0.42</td>
<td>0.3</td>
<td>0.1150</td>
</tr>
<tr>
<td>30</td>
<td>0.42</td>
<td>18.0</td>
<td>0.1152</td>
</tr>
<tr>
<td>30</td>
<td>0.42</td>
<td>48.0</td>
<td>0.1160</td>
</tr>
<tr>
<td>30</td>
<td>0.42</td>
<td>75.0</td>
<td>0.1159</td>
</tr>
<tr>
<td>50</td>
<td>0.42</td>
<td>0.9</td>
<td>0.1156</td>
</tr>
<tr>
<td>75</td>
<td>0.42</td>
<td>0.9</td>
<td>0.1158</td>
</tr>
<tr>
<td>80</td>
<td>0.42</td>
<td>0.9</td>
<td>0.1129</td>
</tr>
</tbody>
</table>

Considering these results, discuss the optimum conditions for determining Mo by this method. Express your results for the precipitant as the minimum %w/v in excess, needed to ensure a quantitative precipitation.

12. A sample of an impure iron ore is approximately 55% w/w Fe. The amount of Fe in the sample is to be determined gravimetrically by isolating it as \(Fe_2O_3\). What mass of sample do you need to ensure that you isolate at least 1 g of \(Fe_2O_3\)?

13. The concentration of arsenic in an insecticide is determined gravimetrically by precipitating \( \text{MgNH}_4\text{AsO}_4 \) and isolating \( \text{Mg}_2\text{As}_2\text{O}_7 \). Determine the \%w/w \( \text{As}_2\text{O}_3 \) in a 1.627-g sample of insecticide if it yields 106.5 mg of \( \text{Mg}_2\text{As}_2\text{O}_7 \).

14. After preparing a sample of alum, \( \text{K}_2\text{SO}_4\cdot\text{Al}_2(\text{SO}_4)_3\cdot24\text{H}_2\text{O} \), a student determined its purity by dissolving a 1.2391-g sample and precipitating the aluminum as \( \text{Al(OH)}_3 \). After filtering, rinsing, and igniting, 0.1357 g of \( \text{Al}_2\text{O}_3 \) is obtained. What is the purity of the alum preparation?

15. To determine the amount of iron in a dietary supplement, a random sample of 15 tablets weighing a total of 20.505 g was ground into a fine powder. A 3.116-g sample was dissolved and treated to precipitate the iron as \( \text{Fe(OH)}_3 \). The precipitate was collected, rinsed, and ignited to a constant weight as \( \text{Fe}_2\text{O}_3 \), yielding 0.355 g. Report the iron content of the dietary supplement as g \( \text{FeSO}_4\cdot7\text{H}_2\text{O} \) per tablet.

16. A 1.4639-g sample of limestone was analyzed for Fe, Ca, and Mg. The iron was determined as \( \text{Fe}_2\text{O}_3 \) yielding 0.0357 g. Calcium was isolated as \( \text{CaSO}_4 \), yielding a precipitate of 1.4058 g, and Mg was isolated as 0.0672 g of \( \text{Mg}_2\text{As}_2\text{O}_7 \). Report the amount of Fe, Ca, and Mg in the limestone sample as \%w/w \( \text{Fe}_2\text{O}_3 \), \%w/w \( \text{CaO} \), and \%w/w \( \text{MgO} \).

17. The number of ethoxy groups \( (\text{CH}_3\text{CH}_2\text{O})^- \) in an organic compound is determined by the following two reactions.

\[
\begin{align*}
\text{R(CH}_2\text{CH}_3)_x &+ x\text{HI} \rightarrow \text{R(OH)}_x + x\text{CH}_3\text{CH}_2\text{I} \\
\text{CH}_3\text{CH}_2\text{I} + \text{Ag}^+ + \text{H}_2\text{O} &\rightarrow \text{AgI(s)} + \text{CH}_3\text{CH}_2\text{OH}
\end{align*}
\]

A 36.92-mg sample of an organic compound with an approximate molecular weight of 176 was treated in this fashion, yielding 0.1478 g of AgI. How many ethoxy groups are there in each molecule of the compound?

18. A 516.7-mg sample containing a mixture of \( \text{K}_2\text{SO}_4 \) and \( (\text{NH}_4)_2\text{SO}_4 \) was dissolved in water and treated with \( \text{BaCl}_2 \), precipitating the \( \text{SO}_4^{2-} \) as \( \text{BaSO}_4 \). The resulting precipitate was isolated by filtration, rinsed free of impurities, and dried to a constant weight, yielding 863.5 mg of \( \text{BaSO}_4 \). What is the \%w/w \( \text{K}_2\text{SO}_4 \) in the sample?

19. The amount of iron and manganese in an alloy can be determined by precipitating the metals with 8-hydroxyquinoline, \( \text{C}_9\text{H}_7\text{NO} \). After weighing the mixed precipitate, the precipitate is dissolved and the amount of 8-hydroxyquinoline determined by another method. In a typical analysis a 127.3-mg sample of an alloy containing iron, manga-
nese, and other metals was dissolved in acid and treated with appropriate masking agents to prevent an interference from other metals. The iron and manganese were precipitated and isolated as Fe(C$_9$H$_6$NO)$_3$ and Mn(C$_9$H$_6$NO)$_2$, yielding a total mass of 867.8 mg. The amount of 8-hydroxyquinolate in the mixed precipitate was determined to be 5.276 mmol. Calculate the %w/w Fe and %w/w Mn in the alloy.

20. A 0.8612-g sample of a mixture of NaBr, NaI, and NaNO$_3$ was analyzed by adding AgNO$_3$ and precipitating a 1.0186-g mixture of AgBr and AgI. The precipitate was then heated in a stream of Cl$_2$, converting it to 0.7125 g of AgCl. Calculate the %w/w NaNO$_3$ in the sample.

20. The earliest determinations of elemental atomic weights were accomplished gravimetrically. In determining the atomic weight of manganese, a carefully purified sample of MnBr$_2$ weighing 7.16539 g was dissolved and the Br$^-$ precipitated as AgBr, yielding 12.53112 g. What is the atomic weight for Mn if the atomic weights for Ag and Br are taken to be 107.868 and 79.904, respectively?

22. While working as a laboratory assistant you prepared 0.4 M solutions of AgNO$_3$, Pb(NO$_3$)$_2$, BaCl$_2$, KI and Na$_2$SO$_4$. Unfortunately, you became distracted and forgot to label the solutions before leaving the laboratory. Realizing your error, you label the solutions A–E and perform all possible binary mixings of the five solutions, obtaining the results shown in Figure 8.16 (key: NP means no precipitate formed, W means a white precipitate formed, and Y means a yellow precipitate formed). Identify solutions A–E.

23. A solid sample has approximately equal amounts of two or more of the followingsoluble salts: AgNO$_3$, ZnCl$_2$, K$_2$CO$_3$, MgSO$_4$, Ba(C$_2$H$_3$O$_2$)$_2$, and NH$_4$NO$_3$. A sample of the solid, sufficient to give at least 0.04 moles of any single salt, was added to 100 mL of water, yielding a white precipitate and a clear solution. The precipitate was collected and rinsed with water. When a portion of the precipitate was placed in dilute HNO$_3$ it completely dissolved, leaving a colorless solution. A second portion of the precipitate was placed in dilute HCl, yielding a precipitate and a clear solution. Finally, the filtrate from the original precipitate was treated with excess NH$_3$, yielding a white precipitate. Identify the salts that must be present in the sample, the salts that must be absent and the salts for which there is insufficient information to make this determination.

24. Two methods have been proposed for the analysis of sulfur in impure samples of pyrite, FeS$_2$. Sulfur can be determined in a direct analysis by

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oxidizing it to $SO_4^{2–}$ and precipitating it as $BaSO_4$. An indirect analysis is possible if the iron is precipitated as $Fe(OH)_3$ and isolated as $Fe_2O_3$. Which of these methods will provide a more sensitive determination for sulfur? What other factors should you consider in choosing between these methods?

25. A sample of impure pyrite known to be approximately 90–95% w/w FeS$_2$ is to be analyzed by oxidizing the sulfur to $SO_4^{2–}$ and precipitating it as $BaSO_4$. How many grams of the sample must you take to form at least 1 g of $BaSO_4$?

26. A series of samples containing any possible combination of KCl, NaCl, and NH$_4$Cl is to be analyzed by adding AgNO$_3$ and precipitating AgCl. What is the minimum volume of 5% w/v AgNO$_3$ necessary to completely precipitate the chloride in any 0.5-g sample?

27. If a precipitate of known stoichiometry does not form, a gravimetric analysis is still feasible if we can establish experimentally the mole ratio between the analyte and the precipitate. Consider, for example, the precipitation gravimetric analysis of Pb as $PbCrO_4$.\(^{14}\)

(a) For each gram of Pb, how many grams of $PbCrO_4$ should form?

(b) In a study of this procedure, Grote found that 1.568 g of $PbCrO_4$ formed for each gram of Pb. What is the apparent stoichiometry between Pb and $PbCrO_4$?

(c) Does failing to account for the actual stoichiometry lead to a positive determinate error or a negative determinate error?

28. Determine the uncertainty for the gravimetric analysis described in Example 8.1. The expected accuracy for a gravimetric method is 0.1–0.2%. What additional sources of error might account for the difference between your estimated uncertainty and the expected accuracy?

29. A 38.63-mg sample of potassium ozonide, KO$_3$, was heated to 70°C for 1 h, undergoing a weight loss of 7.10 mg. A 29.6-mg sample of impure KO$_3$ experiences a 4.86-mg weight loss when treated under similar condition. What is the %w/w KO$_3$ in the sample?

30. The water content of an 875.4-mg sample of cheese was determined with a moisture analyzer. What is the %w/w H$_2$O in the cheese if the final mass was found to be 545.8 mg?

31. Representative Method 8.2 describes a procedure for determining Si in ores and alloys. In this analysis a weight loss of 0.21 g corresponds to 0.1 g of Si. Show that this relationship is correct.

32. The iron in an organometallic compound was determined by treating a 0.4873-g sample with HNO$_3$ and heating to volatilize the organic material. After ignition, the residue of Fe$_2$O$_3$ weighed 0.2091 g.

(a) What is the %w/w Fe in this compound?

(b) The carbon and hydrogen in a second sample of the compound were determined by a combustion analysis. When a 0.5123-g sample was carried through the analysis, 1.2119 g of CO$_2$ and 0.2482 g of H$_2$O were collected. What are the %w/w C and %w/w H in this compound and what is the compound's empirical formula?

33. A polymer's ash content is determined by placing a weighed sample in a Pt crucible that has been previously brought to a constant weight. The polymer is melted under gentle heating from a Bunsen burner until the volatile vapor ignites. The polymer is allowed to burn until only a non-combustible residue remains. The residue is brought to constant weight at 800 °C in a muffle furnace. The following data were collected during the analysis of two samples of a polymer resin.

<table>
<thead>
<tr>
<th>Polymer</th>
<th>g crucible</th>
<th>g crucible + polymer</th>
<th>g crucible + ash</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>replicate 1</td>
<td>19.1458</td>
<td>21.2287</td>
<td>19.7717</td>
</tr>
<tr>
<td>replicate 2</td>
<td>15.9193</td>
<td>17.9522</td>
<td>16.5310</td>
</tr>
<tr>
<td>replicate 3</td>
<td>15.6992</td>
<td>17.6660</td>
<td>16.2909</td>
</tr>
<tr>
<td>B</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>replicate 1</td>
<td>19.1457</td>
<td>21.0693</td>
<td>19.7187</td>
</tr>
<tr>
<td>replicate 2</td>
<td>15.6991</td>
<td>12.8273</td>
<td>16.3327</td>
</tr>
<tr>
<td>replicate 3</td>
<td>15.9196</td>
<td>17.9037</td>
<td>16.5110</td>
</tr>
</tbody>
</table>

(a) For each polymer, determine the mean and the standard deviation for the %w/w ash.

(b) Is there any evidence at $\alpha = 0.05$ for a significant difference between the two polymers? See the appendices for statistical tables.

34. In the presence of water vapor the surface of zirconia, ZrO$_2$, chemically adsorbs H$_2$O, forming surface hydroxyls, ZrOH (additional water is physically adsorbed as H$_2$O). When heated above 200 °C, the surface hydroxyls convert to H$_2$O(g), releasing one molecule of water for every two surface hydroxyls. Below 200 °C only physically absorbed water is lost. Nawrocki, et al. used thermogravimetry to determine the density of surface hydroxyls on a sample of zirconia that was heated to 700 °C and cooled in a desiccator containing humid N$_2$. Heating the sample from 200 °C to 900 °C released 0.006 g of H$_2$O for every gram of dehydroxylated ZrO$_2$. Given that the zirconia had a surface area of 33 m$^2$/g.

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and that one molecule of \( H_2O \) forms two surface hydroxyls, calculate the density of surface hydroxyls in \( \mu \text{mol/m}^2 \).

35. The concentration of airborne particulates in an industrial workplace was determined by pulling the air through a single-stage air sampler equipped with a glass-fiber filter. The air was sampled for 20 min at a rate of 75 m\(^3\)/h. At the end of the sampling period, the filter’s mass was found to have increased by 345.2 mg. What is the concentration of particulates in the air sample in mg/m\(^3\) and mg/L?

36. The fat content of potato chips is determined indirectly by weighing a sample before and after extracting the fat with supercritical \( \text{CO}_2 \). The following data were obtained for the analysis of potato chips.\(^{16}\)

<table>
<thead>
<tr>
<th>Sample Number</th>
<th>Initial Mass (g)</th>
<th>Final Mass (g)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1.1661</td>
<td>0.9253</td>
</tr>
<tr>
<td>2</td>
<td>1.1723</td>
<td>0.9252</td>
</tr>
<tr>
<td>3</td>
<td>1.2525</td>
<td>0.9850</td>
</tr>
<tr>
<td>4</td>
<td>1.2280</td>
<td>0.9562</td>
</tr>
<tr>
<td>5</td>
<td>1.2837</td>
<td>1.0119</td>
</tr>
</tbody>
</table>

(a) Determine the mean and standard deviation for the %w/w fat.

(b) This sample of potato chips is known to have a fat content of 22.7% w/w. Is there any evidence for a determinate error at \( \alpha = 0.05 \)? See the appendices for statistical tables.

37. Delumyea and McCleary reported results for the %w/w organic material in sediment samples collected at different depths from a cove on the St. Johns River in Jacksonville, FL.\(^{17}\) After collecting a sediment core, they sectioned it into 2-cm increments. Each increment was treated using the following procedure:

(a) The sediment was placed in 50 mL of deionized water and the resulting slurry filtered through preweighed filter paper;

(b) The filter paper and the sediment were placed in a preweighed evaporating dish and dried to a constant weight in an oven at 110\(^\circ\)C;

(c) The evaporating dish containing the filter paper and the sediment were transferred to a muffle furnace where the filter paper and any organic material in the sample were removed by ashing;

(d) Finally, the inorganic residue remaining after ashing was weighed.

Using the following data, determine the %w/w organic material as a function of the average depth for each increment.

\(^{16}\) Fat Determination by SFE, ISCO, Inc. Lincoln, NE.
<table>
<thead>
<tr>
<th>Depth (cm)</th>
<th>Filter Paper</th>
<th>Dish</th>
<th>After Drying</th>
<th>After Ashing</th>
</tr>
</thead>
<tbody>
<tr>
<td>0–2</td>
<td>1.590</td>
<td>43.21</td>
<td>52.10</td>
<td>49.49</td>
</tr>
<tr>
<td>2–4</td>
<td>1.745</td>
<td>40.62</td>
<td>48.83</td>
<td>46.00</td>
</tr>
<tr>
<td>4–6</td>
<td>1.619</td>
<td>41.23</td>
<td>52.86</td>
<td>47.84</td>
</tr>
<tr>
<td>6–8</td>
<td>1.611</td>
<td>42.10</td>
<td>50.59</td>
<td>47.13</td>
</tr>
<tr>
<td>8–10</td>
<td>1.658</td>
<td>43.62</td>
<td>51.88</td>
<td>47.53</td>
</tr>
<tr>
<td>10–12</td>
<td>1.628</td>
<td>43.24</td>
<td>49.45</td>
<td>45.31</td>
</tr>
<tr>
<td>12–14</td>
<td>1.633</td>
<td>43.08</td>
<td>47.92</td>
<td>44.20</td>
</tr>
<tr>
<td>14–16</td>
<td>1.630</td>
<td>43.96</td>
<td>58.31</td>
<td>55.53</td>
</tr>
<tr>
<td>16–18</td>
<td>1.636</td>
<td>43.36</td>
<td>54.37</td>
<td>52.75</td>
</tr>
</tbody>
</table>

38. Yao, et al. recently described a method for the quantitative analysis of thiourea based on its reaction with I₂:\(^{18}\)

\[
\text{CS(NH}_2\text{)}_2 + 4\text{I}_2 + 6\text{H}_2\text{O} \rightarrow \text{(NH}_4\text{)}_2\text{SO}_4 + 8\text{HI} + \text{CO}_2
\]

The procedure calls for placing a 100-μL aqueous sample containing thiourea in a 60-mL separatory funnel and adding 10 mL of a pH 7 buffer and 10 mL of 12 μM I₂ in CCl₄. The contents of the separatory funnel are shaken and the organic and aqueous layers allowed to separate. The organic layer, which contains the excess I₂, is transferred to the surface of a piezoelectric crystal on which a thin layer of Au has been deposited. After allowing the I₂ to adsorb to the Au, the CCl₄ is removed and the crystal's frequency shift, Δf, measured. The following data is reported for a series of thiourea standards.

<table>
<thead>
<tr>
<th>[thiourea] (M)</th>
<th>Δf(Hz)</th>
<th>[thiourea] (M)</th>
<th>Δf(Hz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>3.00×10⁻⁷</td>
<td>74.6</td>
<td>1.50×10⁻⁶</td>
<td>327</td>
</tr>
<tr>
<td>5.00×10⁻⁷</td>
<td>120</td>
<td>2.50×10⁻⁶</td>
<td>543</td>
</tr>
<tr>
<td>7.00×10⁻⁷</td>
<td>159</td>
<td>3.50×10⁻⁶</td>
<td>789</td>
</tr>
<tr>
<td>9.00×10⁻⁷</td>
<td>205</td>
<td>5.00×10⁻⁶</td>
<td>1089</td>
</tr>
</tbody>
</table>

(a) Characterize this method with respect to the scale of operation shown in Figure 3.5 of Chapter 3.

(b) Using a regression analysis, determine the relationship between the crystal's frequency shift and the concentration of thiourea.

(c) If a sample containing an unknown amount of thiourea gives a Δf of 176 Hz, what is the molar concentration of thiourea in the sample?

(d) What is the 95% confidence interval for the concentration of thiourea in this sample assuming one replicate? See the appendices for statistical tables.

### 8H Solutions to Practice Exercises

#### Practice Exercise 8.1

The solubility reaction for CaC$_2$O$_4$ is

\[
\text{CaC}_2\text{O}_4(s) \rightleftharpoons \text{Ca}^{2+}(aq) + \text{C}_2\text{O}_4^{2-}(aq)
\]

To minimize solubility, the pH needs to be basic enough that oxalate, C$_2$O$_4^{2-}$, does not react to form H$_2$C$_2$O$_4$ or H$_2$C$_2$O$_4$. The ladder diagram for oxalic acid, including approximate buffer ranges, is shown in Figure 8.17. Maintaining a pH greater than 5.3 ensures that C$_2$O$_4^{2-}$ is the only important form of oxalic acid in solution, minimizing the solubility of CaC$_2$O$_4$.

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#### Practice Exercise 8.2

A conservation of mass requires that all the zinc in the alloy is found in the final product, Zn$_2$P$_2$O$_7$. We know that there are 2 moles of Zn per mole of Zn$_2$P$_2$O$_7$; thus

\[
0.1163 \text{ g Zn}_2\text{P}_2\text{O}_7 \times \frac{2 \text{ mol Zn}}{304.72 \text{ g Zn}_2\text{P}_2\text{O}_7} \times \frac{65.39 \text{ g Zn}}{\text{ mol Zn}} = 4.991 \times 10^{-2} \text{ g Zn}
\]

This is the mass of Zn in 25% of the sample (a 25.00 mL portion of the 100.0 mL total volume). The %w/w Zn, therefore, is

\[
\frac{4.991 \times 10^{-2} \text{ g Zn} \times 4}{0.7336 \text{ g sample}} \times 100 = 27.22\% \text{ w/w Zn}
\]

For copper, we find that

\[
0.1163 \text{ g CuSCN} \times \frac{1 \text{ mol Cu}}{121.64 \text{ g CuSCN}} \times \frac{63.55 \text{ g Cu}}{\text{ mol Cu}} = 0.1249 \text{ g Cu}
\]

\[
\frac{0.1249 \text{ g Cu} \times 4}{0.7336 \text{ g sample}} \times 100 = 67.88\% \text{ w/w Cu}
\]

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Practice Exercise 8.3

The masses of the solids provide us with the following equations

\[ g \text{ NaCl} + g \text{ KCl} = 0.2692 \, \text{g} \]

\[ (g \text{ KClO}_4)_{\text{NaCl}} + (g \text{ KClO}_4)_{\text{KCl}} = 0.5713 \, \text{g} \]

where \((g \text{ KClO}_4)_{\text{NaCl}}\) and \((g \text{ KClO}_4)_{\text{KCl}}\) are the masses of KClO\(_4\) from the reaction of HClO\(_4\) with NaCl and KCl. With two equations and four unknowns, we need two additional equations to solve the problem. A conservation of mass requires that all the chlorine in NaCl is found in the \((g \text{ KClO}_4)_{\text{NaCl}}\); thus

\[ (g \text{ KClO}_4)_{\text{NaCl}} = \frac{g \text{ NaCl} \times \frac{1 \, \text{mol Cl}}{58.44 \, \text{g NaCl}} \times 138.55 \, \text{g KClO}_4}{\text{mol Cl}} \]

\[ (g \text{ KClO}_4)_{\text{NaCl}} = 2.3708 \times g \text{ NaCl} \]

Using the same approach for KCl gives

\[ (g \text{ KClO}_4)_{\text{KCl}} = \frac{g \text{ KCl} \times \frac{1 \, \text{mol Cl}}{74.55 \, \text{g KCl}} \times 138.55 \, \text{g KClO}_4}{\text{mol Cl}} \]

\[ (g \text{ KClO}_4)_{\text{KCl}} = 1.8584 \times g \text{ KCl} \]

Substituting the equations for \((g \text{ KClO}_4)_{\text{NaCl}}\) and \((g \text{ KClO}_4)_{\text{KCl}}\) into the equation for their combined masses leaves us with two equations and two unknowns.

\[ g \text{ NaCl} + g \text{ KCl} = 0.2692 \, \text{g} \]

\[ 2.3708 \times g \text{ NaCl} + 1.8584 \times g \text{ KCl} = 0.5713 \, \text{g} \]

Multiplying the first equation by 1.8584 and subtracting the second equation gives

\[ -0.5124 \times g \text{ NaCl} = -0.07102 \, \text{g} \]

\[ g \text{ NaCl} = 0.1386 \, \text{g} \]

To report the %w/w Na\(_2\)O in the sample, we use a conservation of mass on sodium.

\[ \frac{0.1386 \, g \text{ NaCl} \times \frac{1 \, \text{mol Na}}{58.44 \, g \text{ NaCl}} \times \frac{61.98 \, g \text{ Na}_2\text{O}}{2 \, \text{mol Na}}}{0.8143 \, \text{g sample}} = 0.07350 \, g \text{ Na}_2\text{O} \]

\[ \frac{0.07350 \, g \text{ Na}_2\text{O}}{0.8143 \, g \text{ sample}} \times 100 = 9.026\% \text{ w/w Na}_2\text{O} \]
Practice Exercise 8.4

To find the mass of \((\text{NH}_4)_3\text{PO}_4\cdot12\text{MoO}_3\) producing 0.600 g of \(\text{PbMoO}_3\), we first use a conservation of mass for molybdenum; thus

\[
0.600 \text{ g PbMoO}_3 \times \frac{1 \text{ mol Mo}}{351.14 \text{ g PbMoO}_3} \times \frac{1876.38 \text{ g } (\text{NH}_4)_3\text{PO}_4\cdot12\text{MoO}_3}{12 \text{ mol Mo}} = 0.2672 \text{ g } (\text{NH}_4)_3\text{PO}_4\cdot12\text{MoO}_3
\]

Next, to convert this mass of \((\text{NH}_4)_3\text{PO}_4\cdot12\text{MoO}_3\) to a mass of \(\text{Na}_3\text{PO}_4\), we use a conservation of mass on \(\text{PO}_4^{3-}\).

\[
0.2672 \text{ g } (\text{NH}_4)_3\text{PO}_4\cdot12\text{MoO}_3 \times \frac{1 \text{ mol } \text{PO}_4^{3-}}{1876.38 \text{ g } (\text{NH}_4)_3\text{PO}_4\cdot12\text{MoO}_3} \times \frac{163.94 \text{ g } \text{Na}_3\text{PO}_4}{\text{mol } \text{PO}_4^{3-}} = 0.02335 \text{ g } \text{Na}_3\text{PO}_4
\]

Finally, we convert this mass of \(\text{Na}_3\text{PO}_4\) to the corresponding mass of sample.

\[
0.02335 \text{ g } \text{Na}_3\text{PO}_4 \times \frac{100 \text{ g sample}}{12.5 \text{ g } \text{Na}_3\text{PO}_4} = 0.187 \text{ g sample}
\]

A sample of 0.187 g is sufficient to guarantee 0.600 g of \(\text{PbMoO}_3\). If a sample contains more than 12.5% \(\text{Na}_3\text{PO}_4\), then a 0.187-g sample will produce more than 0.600 g of \(\text{PbMoO}_3\).

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Practice Exercise 8.5

To determine which form has the greatest sensitivity, we use a conservation of mass for iron to find the relationship between the precipitate’s mass and the mass of iron.

\[
g_{\text{FeO}} = g_{\text{Fe}} \times \frac{1 \text{ mol Fe}}{55.85 \text{ g Fe}} \times \frac{71.85 \text{ g FeO}}{\text{mol Fe}} = 1.286 \times g_{\text{Fe}}
\]

\[
g_{\text{Fe}_2\text{O}_3} = g_{\text{Fe}} \times \frac{1 \text{ mol Fe}}{55.85 \text{ g Fe}} \times \frac{159.70 \text{ g Fe}_2\text{O}_3}{2 \text{ mol Fe}} = 1.430 \times g_{\text{Fe}}
\]

\[
g_{\text{Fe}_3\text{O}_4} = g_{\text{Fe}} \times \frac{1 \text{ mol Fe}}{55.85 \text{ g Fe}} \times \frac{231.55 \text{ g Fe}_3\text{O}_4}{3 \text{ mol Fe}} = 1.382 \times g_{\text{Fe}}
\]
Of the three choices, the greatest sensitivity is obtained with Fe$_2$O$_3$ because it provides the largest value for $k$.

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**Practice Exercise 8.6**

From 100–250°C the sample loses 13.8% of its mass, or a loss of

$$0.138 \times 130.35 \text{ g/mol} = 18.0 \text{ g/mol}$$

consistent with the loss of H$_2$O(g), leaving a residue of MgC$_2$O$_4$. From 350–550°C the sample loses 55.23% of its original mass, or a loss of

$$0.5523 \times 130.35 \text{ g/mol} = 71.99 \text{ g/mol}$$

This weight loss is consistent with the simultaneous loss of CO(g) and CO$_2$(g), leaving a residue of MgO.

We can analyze the mixture by heating a portion of the sample to 300°C, 600°C, and 1000°C, recording the mass at each temperature. The loss of mass between 600°C and 1000°C, $\Delta m_2$, is due to the loss of CO$_2$(g) from the decomposition of CaCO$_3$ to CaO, and is proportional to the mass of CaC$_2$O$_4$•H$_2$O in the sample.

$$g \text{ CaC}_2\text{O}_4\cdot\text{H}_2\text{O} = \Delta m_2 \times \frac{1 \text{ mol CO}_2}{44.01 \text{ g CO}_2} \times \frac{146.11 \text{ g CaC}_2\text{O}_4\cdot\text{H}_2\text{O}}{1 \text{ mol CO}_2}$$

The change in mass between 300°C and 600°C, $\Delta m_1$, is due to the loss of CO(g) from CaC$_2$O$_4$•H$_2$O and the loss of CO(g) and CO$_2$(g) from MgC$_2$O$_4$•H$_2$O. Because we already know the amount of CaC$_2$O$_4$•H$_2$O in the sample, we can calculate its contribution to $\Delta m_1$.

$$(\Delta m_1)_{\text{Ca}} = g \text{ CaC}_2\text{O}_4\cdot\text{H}_2\text{O} \times \frac{1 \text{ mol CO}}{146.11 \text{ g CaC}_2\text{O}_4\cdot\text{H}_2\text{O}} \times \frac{28.01 \text{ g CO}}{1 \text{ mol CO}}$$

The change in mass due to the decomposition of MgC$_2$O$_4$•H$_2$O

$$(\Delta m_1)_{\text{Mg}} = (\Delta m_1) - (\Delta m_1)_{\text{Ca}}$$

provides the mass of MgC$_2$O$_4$•H$_2$O in the sample.

$$g \text{ MgC}_2\text{O}_4\cdot\text{H}_2\text{O} = (\Delta m_1)_{\text{Mg}} \times \frac{1 \text{ mol (CO + CO}_2)}{130.35 \text{ g MgC}_2\text{O}_4\cdot\text{H}_2\text{O}} \times \frac{78.02 \text{ g (CO + CO}_2)}{1 \text{ mol (CO + CO}_2)}$$

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Practice Exercise 8.7

In Practice Exercise 8.6 we developed an equation for the mass of CaC$_2$O$_4$•H$_2$O in a mixture of CaC$_2$O$_4$•H$_2$O, MgC$_2$O$_4$•H$_2$O, and inert materials. Adapting this equation to a sample containing CaC$_2$O$_4$, CaC$_2$O$_4$, and inert materials is easy; thus

$$\text{g CaC}_2\text{O}_4 = (0.1794 \text{ g} - 0.1294 \text{ g}) \times \frac{1 \text{ mol CO}_2}{44.01 \text{ g CO}_2} \times \frac{128.10 \text{ g CaC}_2\text{O}_4}{\text{mol CO}_2} = 0.1455 \text{ g CaC}_2\text{O}_4$$

The %w/w CaC$_2$O$_4$ in the sample is

$$\frac{0.1455 \text{ g CaC}_2\text{O}_4}{0.3317 \text{ g sample}} \times 100 = 43.86\% \text{w/w CaC}_2\text{O}_4$$

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